

GCSE Mathematics

93702F Applications of Mathematics Unit 2: Foundation Tier Mark scheme

93702F

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Version V1 Final Mark Scheme

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

М	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
Mdep	A method mark dependent on a previous method mark being awarded.
Bdep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg, accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between a and b inclusive.
3.14	Allow answers which begin 3.14 eg 3.14, 3.142, 3.149.
Use of brackets	It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Q	Answer	Mark	Comments
1(a)	grams	B1	
	grans	ы	
1(b)	kilometres	B1	
		Г Г	
1(c)	square metres	B1	

Q	Answer	Mark	Comments
2(a)	2	B1	
2(b)		B1	Allow if intention clear Must add exactly one hexagon
	or		

Q	Answer	Mark	Comments		
	12 or 16.8(0) or 13.8(0) or (£)1.61 seen	B1	12 could be on diagram		
	their $12 \times 1.4 \times 1.15$ or their 16.8(0) × 1.15 or their 13.8(0) × 1.4	M1			
	19.32	A1ft	ft B0 M1 only		
2(c)	Additional guidance				
	Some candidates round part way through the calculation Examples				
	12 × 1.4 = 16.8 = 17 17 × 1.15 = 19.55			B1M1A0	
	12 × 1.4 = 16.8 17 × 1.15 = 19.55			B1M1A0	

Q	Answer	Mark		Comments		
	16 × 0.45 or 7.2(0) or 16 × 45 or 720	M1				
	10 – their 7.2(0) or 2.8(0) or 1000 – their 720 or 280	M1				
	4 (coins) and £2, 50p, 20p, 10p seen	A2	A1 A1ft	£2, 50p, 20p, 10p seen or more than 4 coins with with number of coins g M2 scored and smalles coins for their £2.80 with coins given	total £2.80 iven st number of	
	A	dditional	guidan	се		
3	All coins must be real					
	To obtain A2 must score M2 and give the four correct coins and 4 (coins)					
	To obtain A1 must score M2 and give the four correct coins					
	To obtain A1ft must score M2 and give the smallest number of coins with total their £2.80 together with the number of coins Examples					
	$16 \times 0.45 = $ £7.20		M1			
	$\pounds 10 - \pounds 7.20 = \pounds 3.80$		M1 A0ft			
	£2, £1, 50p, 20p, 5p and 5p		 			
	$16 \times 0.45 = \pounds 7.20$ $\pounds 10 - \pounds 7.20 = \pounds 3.80$	$16 \times 0.45 = \pounds7.20$ $\pounds10 = \pounds7.20 = \pounds3.80$				
	$\pounds 2, \pounds 1, 50p, 20p, 10p and 5 (coins)$				M1 A1ft	

Q	Answer	Mark	Comments	
4	✓ × ×	B3	B2 3 correct B1 2 correct	
	\checkmark			
	$13\frac{1}{2}$ seen	B1	Attempt at area e.g. counting squares counting squares in 5's	
	their $13\frac{1}{2} \times 5$ or their $13 \times 5 + 2.5$	M1	oe	
5(a)	$67\frac{1}{2}$	A1ft	oe ft B0M1 SC2 840	
	Additional guidance			
	For B1 allow dots or numbers seen in the a value of 13 or 14 if clearly not do not allow dashes on the edges	a perimete		

Q	Answer	Mark	Comments		
5(b)	Line joining midpoints of <i>AB</i> and <i>AD</i>	B2	B1 line joining midpoint of <i>AB</i> to <i>AD</i> or line joining midpoint of <i>AD</i> to <i>AB</i> or midpoints of <i>AB</i> and <i>AD</i> identified		
	Additional guidance				
	Allow an un-ruled line if the intention cle a tolerance of \pm 2 mm at the end				

5(c)	cross 8 squares from C and 4 squares from B allow a tolerance of \pm 2 mm	B2	 B1 cross 8 squares from B and 4 squares from C or 12 ÷ 3 or 4 or 8 seen
5(c)	A Cross must be on the line $BC \pm 2$ mm	dditional g	

Q	Answer	Mark	Comments
6(a)	[104, 106]	B1	
6(b)	[72, 74]	B2	B1 160 (pounds)
			or
			B1ft correct answer from their 160 pounds
			Allow $\pm \frac{1}{2}$ small square
			SC1 70
	Ad	ditional G	uidance

7	Alternative method 1				
	18 × 12 or 216				
	or	M1			
	18 × 12 – 15 or 201				
	their 201 \times 6.25	M1dep	their 201 is not either 216 or 231		
	1256.25	A1			
	Alternative method 2				
	18 × 12 × 6.25 or 1350				
	or	M1			
	15 × 6.25 or 93.75				
	their 1350 – their 93.75	M1dep	must be two amounts of money		
	1256.25	A1			
	Additional Guidance				
	For 18 × 12 + 15 or 231 allow M1 c	only			

Q	Answer	Mark	Comments		
	45 minutes	B3	B2 Job A \rightarrow 2 h or 120 min Job B \rightarrow 1 h 15 min or 75 B2ft Job A \rightarrow 2 h or 120 min and correctly works out in 2 h – their Job B time or Job B \rightarrow 1 h 15 min or 75 and correctly works out in their Job A time – 1 h 1 B1 Job A \rightarrow 2 h or 120 min Job B \rightarrow 1 h 15 min or 75 B1ft their Job A time – their Joc correctly worked out in min	min minutes 5 min 5 min or min ob B time	
	Ad	dditional (Guidance		
8(a)	Decimal time For example Allow 2.00 for 2 hours Allow 1.15 or 1 h 15 for 1 h 15 min only if it is clearly used as 1 h 15 min in a subsequent calculation				
	Examples				
	3.00× - 1.15× = 1.85× = 145 minutes×				
	2.00✓ – 1 h 15× = 0.85× = 85 minutes×				
	$3.00 \times -1 \text{ h} 15 \checkmark = 1.45 \checkmark = 145 \text{ minutes} \times$				
	$3.00 \times -1.15 \checkmark = 1.45 \checkmark = 105 \text{ minutes} \checkmark$				
	$2.00\checkmark - 1.15\checkmark = 0.45\checkmark = 45 \text{ minutes}\checkmark$	/		B3	
	$2.00\checkmark - 1.15\checkmark = 0.45\checkmark$			B2	
	2.00√ – 1.15× = 0.45 h×			B1	

Q	Answer	Mark	Comments		
	Alternative method 1				
	36 ÷ 60 × their 45	M1	oe		
	27	A1ft	ft their 8(a)		
	Alternative method 2				
	their 2 × 36 – their 1.25 × 36	M1	ое		
	27	A1ft	ft their 8(a)		
8(b)	Additional Guidance				
	Follow through				
	For any fraction of an hour in 8(a) could score up to M1A1ft				
	For a whole number of hours in 8(a) could score up to M1 only				
	Decimal times				
	Allow decimal times for M1				
	Examples				
	2 × 36 – 1.15 × 36 = 30.6			M1A0	

9		B2 B1	all correctly shaded on outside or all correctly shaded on inside or as B2 with or without the centre square shaded and up to 12 other squares shaded to give a pattern with rotational symmetry of order 4
	A Ignore the practise grid unless the ans	ditional guida	

Q	Answer	Mark	Comments		
	Two 'vertical' lines from base of length $8 \text{ cm} \pm 0.2 \text{ cm}$	B1			
	Right angles ($\pm 2^{\circ}$) drawn at ends of base	B1			
10	Semicircle of diameter 6 cm \pm 0.2 cm at 'top' of rectangle	B1			
	Additional guidance				

11(a) $3\frac{1}{2}$ or 3.5	B1	
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11(b)	60	B1	
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11(c)	'After leaving Madrid' ticked	B1	Examples of equivalent reasons	
	and		1 steeper line	
	larger gradient		2 same time to travel a longer distance	
			or	
			B1ft 'After leaving Madrid' ticked	
			and	
			their 60 and 90	
	A	dditional g	guidance	
	Only ft if using their 60 from part (b) in	n their reason		

Q	Answer	Mark	Comments			
	Alternative method 1					
	8 km = 5 miles or 1 km = [0.62, 0.63] miles or 1 km = 0.6 miles or 1 mile = [1.6, 1.61] km	B1	May be implied in working oe			
	$104 \div 8 \times 5$ or $104 \times [0.62, 0.63]$ or 104×0.6 or $104 \div [1.6, 1.61]$	M1	Uses their conversion factor oe			
	65 or [64.4, 65.52] or [64.5, 65]	A1	Use value from their M1 calculation			
	Alternative method 2					
11(d)	8 km = 5 miles or 1 km = [0.62, 0.63] miles or 1 km = 0.6 miles or 1 mile = [1.6, 1.61] km	B1	May be implied in working oe			
	60 ÷ 5 × 8 or 60 ÷ [0.62, 0.63] or 60 ÷ 0.6 or 60 × [1.6, 1.61]	M1	Uses their conversion factor oe			
	96 or [95.2, 96.8] or [96, 96.6]	A1	Use value from their M1 calculation			
	Additional guidance					
	For B1 and M1 → allow conversions to 1 decimal place For M1 allow incorrect conversion factors only if they have been stated in the working					
	have not been stated but are in the following ranges 1 km = [0.5, 0.7] miles					
	1 mile = [1.5, 1.7] km but not 1.7 if it is clearly from $104 \div 60 = 1.73$ rounded down For A1 \rightarrow answers must be in the ranges given and be compatible with the conversion factors					
	used Reversing the conversion factor, e.g. using 1 mile = 0.6 km etc, scores B0 but can score M1					

Q	Answer	Mark	Comments		
	1				
	$20 \times 20 \times 20 \times 64 = 512\ 000$ or	Q2	Strand (ii) Correct completion of argument		
	512 000 \div (20 \times 20 \times 20) = 64 or		$Q1 20 \times 20 \times 20$		
	512 000 ÷ 64 = 20 × 20 × 20		or		
	or		20 ³		
	$20^3 \times 64 = 512\ 000$ or		or		
	$512\ 000 \div 20^3 = 64$ or		512 000 ÷ 64		
12(a)	$512\ 000 \div 64 = 20^3$		or		
			8000 seen		
	Additional guidance				
	To score Q2 there must be a clear connection between 8000 and $20 \times 20 \times 20$ or 20^3				
	Example				
	512 000 \div 64 = 8000 and 20 \times 20 \times 20 = 8000 scores Q2				
	1				
	128 × 100 or 12 800	M1	oe		
	40	A1			
12(b)	Additional guidance				

12(0)		
	12 800 × 40 = 512 000	M1A0
	12 800 × 40 = 512 000 Answer 40	M1A1

Q	Answer	Mark	Comments		
12(c)	$128 \div 20$ or 6.4 or 6 or $100 \div 20$ or 5 or their $40 \div 20$ or 2 their $6 \times$ their $5 \times$ their 2 or 6 and 5 and 2	M1	or $20 \times 6 = 120$ or $20 \times 5 = 100$ or $20 \times 2 = 40$ their 6 and their 5 and their 2 must be integers and rounded up or down their 2 is the answer to their $40 \div 20$ rounded up or down		
	60	A1ft	ft their 40		
	Additional guidance				
	Check for correct integers on the diagram for M1 or M1M1				

	210 ÷ 6 × 4 or	M1	oe	
	210 ÷ 3 or 70 and 210 – their 70			
	140	A1		
Additional guidance				
13	13 Using $\frac{2}{3}$ (or $\frac{4}{6}$) as a decimal			
		M1A0		
210 × 0.6666 = 139.986 or 210 × 0.6667 = 140.007 with rounded answe				M1A0
	210 × 0.6666 with answer 140	M1A1		
	210 × 0.6 = 126			MOAO

Q	Answer	Mark	Comments			
	3×9 has a units digit of 7 or $3 \times 9 = 27$	B1	oe			
	Additional guidance					
4.4(-)	Ignore further work if not contradictory Example					
14(a)	3 and 9 are both prime and $3 \times 9 = 27$					
	Allow equivalent answers Examples					
	13 × 19 = 247					
	$27 \div 9 = 3 \text{ or } 247 \div 13 = 19$					

14(b)	89 and 73	B2	B1	two prime numbers that multiply to give an integer with units digit 7 e.g. 1 83 and 79 e.g. 2 31 and 37 e.g. 3 $17 \times 11 = 187$ e.g. 4 $43 \times 19 = 817$ or divides 6497 by a prime number other than 2 or 5
	A	dditional g	uida	nce
	The answer to a multiplication or division	on need no	t be s	hown
	Award B1 for one correct in a list of res	ponses		
	If 14(b) is blank check 14(a) and award	l any availa	ble n	narks

Q	Answer	Mark	Comments	
15(a)	5x = 2x + 12	B1		
	4	B2ft	B1ft $3x = 12$ oe ft their equation from (a) for B2 or B1	
	A	dditional g	Juidance	
	If $5x = 2x + 6$ or $2x = 5x - 6$ in part (a) $\rightarrow 2$ scores B2 and $3x = 6$ oe scores B1			
	If $5x = x + 12$ in part (a) $\rightarrow 3$ scores B2 and $4x = 12$ oe scores B1			
15(b)	If 0 marks are scored in (a) The correct solution for any equation in (a) can score up to B2			
	If 1 mark is scored in (a) The correct solution for any equation other than $5x = 2x + 12$ in (a) can score B1 max			
	Award B1ft for the correct rearrangement of the equation separating <i>x</i> terms and numbers on opposite sides of the equation, e.g. $5x - x = 12$ from $5x = x + 12$			
	Answers only			
	Answer 4 only always scores B2			
	Answer 2 only or answer 3 only scores	B2 only if	it is compatible with their answer to 15(a)	

Q	Ans	wer	Mark	Comments	
	Alternative method 1				
	54		B1ft	 ft 9x + 18 evaluated correctly for their value of x in (b) Only ft their value of x in (b) 	
	their 54 and 50 an	d Vaa	Q1ft		
	their 54 and 50 an	u res	QIII	only ft their value of x in (b) Strand (iii) Correct evaluation of $9x + 18$ with correct ft decision made	
				SC1 their 48 and 50 and correct decision	
	Alternative metho	od 2			
	Alternative method 2 54 their 10.8 and Yes or or		B1ft	ft $9x + 18$ evaluated correctly for their value of x in (b)	
				only ft their value of x in (b)	
	their 10.8 and Yes	their 5.4 and Yes	Q1ft	only ft their value of x in (b)	
15(c)	or their 54 ÷ 5 = 10 and Yes	or their 54 ÷ 10 = 5 and Yes		Strand (iii) Correct evaluation of $9x + 18$ and correct evaluation of their $54 \div 5$ or their $54 \div 10$ with correct ft decision made	
				SC1 their 9.6 and correct decision	
				or	
				their $48 \div 5 = 9$ and correct decision	
				or	
				their 4.8 and correct decision	
				or	
				their $48 \div 10 = 4$ and correct decision	
	Additional guidance				
	Alternative method	$1 \rightarrow must see 50 a$	s well as th	neir 54 and correct ft decision for Q1ft	
	Decision may be implied \rightarrow e.g. 54 > 50 does not imply yes				
	If the numbers of a	apples in bags C and	I D are equ	ual allow either $12x + 6$ or $6x + 30$ for $9x + 18$	
	their 48 \rightarrow the correct evaluation of 9x + 12 for their x				

Q	Answer	Mark	Comment	ts	
16(a)	[228, 232]	B1			
	36 + 39 or 75	M1			
	their [9.8, 10.2] × 5 or [49, 51]	M1			
	[24, 26]	A1	SC1 16		
	Additional guidance				
	2 nd M1				
	their [9.8, 10.2] × 5 or [49, 51] can be				
16(b)	$CD \rightarrow [5.8, 6.2] \times 5$ or [29, 31]				
10(b)	$BC \text{ or } AD \rightarrow [6.4, 6.8] \times 5 \text{ or } [32, 34]$				
	$AB \rightarrow [8.8, 9.2] \times 5$ or [44, 46]				
	$BD \rightarrow [9.6, 10] \times 5$ or [48, 50]				
	If a length is measured incorrectly and the incorrect length is stated and linked then their [9.8, 10.2] can be the given incorrect length The link could be on the diagram.				
	Example				
	AC = 10.5 or AC drawn with 10.5 next to it on diagram				
	$10.5 \times 5 = 52.5$ and $36 + 39 = 75$ M1M1A0				
	75 – 52.5 = 22.5				

17(a)	$A \rightarrow 3$	B2	B1	Any two or three correct
	and			
	$B \rightarrow 2$			
	and			
	$C \rightarrow 4$			
	and			
	$D \rightarrow 1$			
·			1	

17(b)	(Graph) 3	B1	Allow A and 3
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Q	Answer	Mark	Comments		
18(a)	Straight line joining (0, 40) and (100, 70) Allow $\pm \frac{1}{2}$ small square at (0, 40) and at (100, 70)	B2	 B1 straight line with positive gradient passing through (0, 40) or straight line with positive gradient passing through (100, 70) or straight line with gradient 0.3 or coordinates of any two points on line identified on graph or in working 		
	Additional guidance				
	To check gradient use their endpoints. Allow tolerance [0.28, 0.32]. B2 \rightarrow their line must span 0 cards to 100 cards				

	Alternative method 1			
	56 or their [54, 56]	M1	ft their graph for [54, 56] from 50 cards Allow $\pm \frac{1}{2}$ small square	
	[110, 112]	A1ft	ft 56 + their [54, 56]	
18(b)	Alternative method 2			
18(b)	56 or 40 + 0.3 × 50 or 55	M1	oe, e.g. 40 + 3 × 5	
	111	A1		
	Additional guidance			
	Alternative method 1			
	their 55 can be from a horizontal lir	ne e.g. charge	= 40, a line with negative gradient or a curve	

Q	Ans	swer	Mark	Comments			
	Alternative metho	od 1					
	50 + 0.6 × 150 or 50 + 6 × 15 or 90	(130 – 50) ÷ 0.6	M1	oe, e.g. 110 + 0.6 × 50 or 110 + 6 × 5			
	(150 cards cost) (£)140 and No	(Only) 133 (.3) (cards) (can be bought for £130) and No	A1				
	Alternative metho	od 2					
18(c)	110 + 80 - 50 (from 100 cards - and 50 cards = (£)80)	→ (£)110	M1	oe, e.g. $2 \times 95 - 50$ (from 75 cards \rightarrow £95) or $3 \times 80 - 2 \times 50$ (from 50 cards \rightarrow £80)			
10(0)	(150 cards cost) (s	E)140 and No	A1				
	Alternative metho	od 3					
	$(100 \text{ (cards)} \rightarrow \text{(£)})$ $110 \text{ (cards)} \rightarrow \text{(£)})$ $120 \text{ (cards)} \rightarrow \text{(£)})$ $130 \text{ (cards)} \rightarrow \text{(£)})$ $(140 \text{ (cards)} \rightarrow \text{(£)})$ $(150 \text{ (cards)} \rightarrow \text{(£)})$	116 122 128)134)	M1	oe, e.g. 130 (cards) → (£)128 implies all previous values			
	(150 cards cost) (4 or (140 cards cost) (4		A1	or $130 \text{ cards} \rightarrow (\pounds)128 \text{ and } No \rightarrow \pounds2 \text{ is}$ not enough (to buy 20 more cards) oe or $130 \text{ cards} \rightarrow (\pounds)128 \text{ and } No \rightarrow \pounds2 \text{ can}$ only buy 3 more cards oe			
		A	dditional	guidance			
	Decision (No) mus	st be seen for A1					

Q	Answer	Mark	Comments		
	30 ÷ 24 or 6 ÷ 24 or 15 (min) or 0.25 or 60 ÷ 24 × 30	M1	oe		
	1.25 (h) or 75 (min)	A1	oe		
	1 h 15 min	B1ft	ft their time SC2 1 h 25 min		
	Additional guidance				
19(a)	Do not award B1ft if their time is a whole number of h if their time is in minutes < 60 min Examples	nours			
	24 ÷ 30 = 0.8 = 80 min = 1 h 20 min				
	24 ÷ 30 = 0.8 = 1 h 20 min				
	24 ÷ 30 = 0.8 (0.8 × 60 =) 48 min			M0A0B1ft	

Q	Answer	Mark	Comments		
	$16^2 + 30^2$ or 256 + 900 or 1156	M1			
	$\sqrt{16^2 + 30^2}$	M1dep			
	34	A1	SC1 [25.3, 25.4]		
	Additional guidance				
19(b)	Example 1				
19(0)	32 + 60 = 92 $\sqrt{92} = 9.59$		MOM	0A0	
	Example 2		· · · ·		
	$16^2 = 32$ and $30^2 = 60$ 32 + 60 = 92 $\sqrt{92} = 9.59$		M1M	1A0	