



GCSE

Mathematics

93701H Applications of Mathematics

Unit 1: Higher Tier

Mark scheme

93701H

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Version 1.0 Final.

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts. Alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this mark scheme are available from aqa.org.uk

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

| | |
|------------------------|--|
| M | Method marks are awarded for a correct method which could lead to a correct answer. |
| A | Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working following a mistake in an earlier step. |
| SC | Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth. |
| M dep | A method mark dependent on a previous method mark being awarded. |
| B dep | A mark that can only be awarded if a previous independent mark has been awarded. |
| oe | Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$ |
| [a, b] | Accept values between a and b inclusive. |
| 3.14... | Allow answers which begin 3.14 eg 3.14, 3.142, 3.149. |
| Use of brackets | It is not necessary to see the bracketed work to award the marks. |

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| Q | Answer | Mark | Comments |
|-------------|--|--------|--------------------------|
| 1(a) | Alternative method 1 | | |
| | 0.15 × 275 or 41.25 | M1 | oe |
| | 275 – their 41.25 | M1dep | |
| | 233.75 | A1 | |
| | Additional guidance | | Mark |
| | For a build up method the complete build up must be seen for M1 Condone 233.75 seen in working followed by 41.25 on answer line | | M2 A1 |
| | Alternative method 2 | | |
| | 0.85 seen | M1 | |
| | 0.85 × 275 | M1dep | |
| | 233.75 | A1 | |
| 1(b) | 0.35 | B1 | |
| 2(a) | 1.44 | B1 | |
| | Additional guidance | | |
| | Allow £1.44p | | |
| 2(b) | 268 ÷ 134 or 2 | M1 | £2 per 1% of CPI |
| | their 2 × 107 | M1 dep | |
| | 214 | A1 | |
| 3 | A - 2 B - 3 C - 1 | B2 | B1 for one correct match |
| | Additional guidance | | |
| | Do not condone letters used for 1, 2, and 3 | | |

| Q | Answer | Mark | Comments |
|---|--|------|---|
| 4 | Alternative method 1 | | |
| | $\frac{54}{75} (\times 100)$ or $\frac{45}{60} (\times 100)$ | M1 | oe |
| | 72(%) and 75(%) or (Paper 1 75% of 75 =) 56.25 or (Paper 2 72% of 60 =) 43.2 | A1 | |
| | (Paper) 2 | Q1ft | ft their percentages or decimals if M1 gained and at least one value is correct |
| | Alternative method 2 | | |
| | Changes to decimals or equivalent fractions 0.72 or 0.75 or $\frac{216}{300}$ or $\frac{225}{300}$ | M1 | oe |
| | Changes to decimals or equivalent fractions 0.72 and 0.75 or $\frac{216}{300}$ and $\frac{225}{300}$ | A1 | Allow any equivalent fractions |
| | (Paper) 2 | Q1ft | ft their percentages or decimals if M1 gained and at least one value is correct |

| Q | Answer | Mark | Comments |
|---|--|------|---------------|
| 4 (cont.) | Additional guidance | | Mark |
| | For Q1 their values must be compared in the same format with at least one correct. Any equivalent fractions are acceptable eg $\frac{432}{600}$ and $\frac{450}{600}$ and Paper 2 | | M1A1Q1 |
| 5(a) | It is cheaper/quicker (than testing the population) Too expensive to test them all or too time consuming to test them all | B1 | oe |
| | Additional guidance | | Mark |
| Accept any equivalent comment that recognises a sample is better than a Population If referring to too long or too expensive they must state 'to test the population' Because it would take too long and would be too expensive Because testing the population would take too long | | | B0 B1 |
| 5(b) | Sample size is too small | B1 | |
| | Only one day/ time of day or only test one week or not random | B1 | |
| | Additional guidance | | Mark |
| Both comments may be seen and marked under criticism 1 or 2 | | | |

| Q | Answer | Mark | Comments | |
|---|--|--------|---|-------------|
| 6 | Women rail 112 ÷ 4 or 28 | B1 | | |
| | 0.3 × 200 or 60 | M1 | oe | |
| | their 60 ÷ 4 | M1 dep | May be implied by 45 or 15 seen | |
| | Road (Women 45) (men) 15 | A1 | | |
| | 200 – 112 – 37 – their 15 or 36 | M1 | or 200 – their 60 – 37 – their 39 (women air) | |
| | 64 | A1ft | Ft their 36 + their 28 or ft their 60 and their 39 used | |
| | Additional guidance | | | Mark |
| | Work may be seen in a two way table or in the space or working lines | | | |

| Q | Answer | Mark | Comments |
|---|---|------|--|
| 7(a) | midpoints used correctly | B1 | condone one error |
| | $(12.5 \times 17) + (17.5 \times 46) + (22.5 \times 22)$ $+ (27.5 \times 10) + (32.5 \times 5)$ or $212.5 + 805 + 495 + 275 + 162.5$ or 1950 | M1 | Attempt at $\sum fx$ using values on or between class boundaries |
| | their $1950 \div 100$ | M1 | |
| | 19.5 | A1 | SC2 17 or 22 |
| Additional guidance | | | Mark |
| For 2 nd method mark allow their 100 if totalling $\sum f$ clearly seen 17 and 22 come from use of lower and upper class boundaries | | | |
| 7(b) | Yes because the average speed was less than 20 or Yes as 63 cars/ about 2/3 of cars/most cars/over half the cars drive at or below 20 or No, as 37 cars break the speed limit | B1ft | Ft their answer to part (a) oe |

| Q | Answer | Mark | Comments |
|---|--|------|--|
| 8 | $2(x + 12)$ or $2x + 24$ seen | B1 | |
| | $x + \text{their } (x + 12) + \text{their } 2(x + 12) = 204$ | M1 | Setting up their equation. Must include 3 terms in x |
| | $4x = 168$ or $x = \frac{\text{their } 168}{4}$ | M1 | Rearranging to a single term Ft their collection of like terms. |
| | 42 | A1 | |
| | Organised algebraic response | Q1 | Must gain 2 nd and 3rd method marks. QWC strand ii SC3 42 from a numerical/T&I approach. SC3 56 from an algebraic approach |
| Additional guidance | | | |
| <p>$4x + 36 = 204$ is B1M1</p> <p>The Q mark is for an algebraic method leading to their solution</p> <p>Example</p> <p>Condone one arithmetical slip for the second Method mark-eg $204 - 36 = 176$</p> <p>Adding 36 instead of subtracting 36 is not an arithmetical error – it is incorrect method</p> <p>Example</p> <p>$4x + 36 = 204$</p> <p>$204 - 36 = 168$</p> <p>$168 \div 4 = 42$</p> <p>B1 (implied) M1M1A1Q1</p> <p>Special cases</p> <p>If SC3 is awarded for 42 for T & I. do not award the B1 even if correct expressions seen for Phil.</p> <p>Omission of Ben or incorrect use of brackets (for Phil) may lead to the equation $3x + 36 = 204$</p> <p>Solved correctly gives an answer of 56 for SC3</p> | | | |

| Q | Answer | Mark | Comments |
|--------------|--|-------|---|
| 9(a) | (0), 5, 18, 38, 63, 78, 90 | B1 | Correct cf values – may be implied by correct heights on graph |
| | Plotting at upper class boundaries | B1 | Must be an increasing graph |
| | 3 or 4 of their cf heights correct | B1 ft | ft first B1. Must be an increasing graph |
| | All their heights correct and points joined with a smooth curve or straight lines starting at (40, 0) | B1 | Must be an increasing graph Ignore any additional graph underneath. |
| 9(b) | median = '73' | B1 | Ft their increasing graph |
| | Their upper quartile – their lower quartile | M1 | Ft their increasing graph with at least one value correct for their graph |
| | '21' | A1 ft | Ft their increasing graph |
| 9(c) | Correct comment using the median eg he is not correct as the median/average mass of his apples is lower than Lucy's | B1 ft | Ft their median |
| | Correct comment using the IQR eg his apples vary more in mass than Lucy's apples | B1 ft | Ft their IQR |
| 10(a) | x is the number of 10p coins and y is the number of 20p coins | B1 | |
| 10(b) | $x + y = 35$ or $y + x = 35$ | B1 | |
| 10(c) | $x + 2y = 56$ and $x + y = 35$ or $10x + 20y = 560$ and $10x + 10y = 350$ | M1 | oe equating coefficients of x or y Allow one error in totals |
| | $y = 21$ | A1 | |
| | $x = 14$ | A1 | SC1 for $x=14$ and $y=21$ using T & I or with no working. |

| Q | Answer | Mark | Comments | |
|----|--|------|--|------------------------------|
| 11 | 9.5 or 10.5 or 47.5 or 52.5 | B1 | | |
| | 10.5 and 52.5 | B1 | | |
| | their 52.5 × their 10.5 | M1 | Multiplying their upper bounds. Their upper bounds cannot be 50 and/or 10 | |
| | 551.25(tonnes) | A1ft | ft if they multiply their upper bounds | |
| | Additional guidance | | | Mark |
| | eg, $55 \times 10.5 = 577.5$ | | | B1B0M1 A1ft |
| 12 | Alternative method 1 | | | |
| | 12 000 linked to 1.3% or 16 000 linked to 1.4% | B1 | Implied by use of digits 13 or 14 eg 12000×1.3 | |
| | $12\ 000 \times 1.013$ or $16\ 000 \times 1.014$ | M1 | | |
| | 12 156 and 16 224 | A1 | Either of these values implies B1 M1 | |
| | their 224 – their 156 | M1 | subtracting the two amounts of interest | |
| | (£)68 | A1 | | |
| | Alternative method 2 | | | |
| | 12 000 linked to 1.3% or 16 000 linked to 1.4% | B1 | Implied by use of digits 13 or 14 eg 12000×1.3 | |
| | $12\ 000 \times 0.013$ or $16\ 000 \times 0.014$ | M1 | working out just the interest | |
| | 156 and 224 | A1 | Either of these values implies B1 M1 | |
| | their 224 – their 156 | M1 | | |
| | (£)68 | A1 | | |

| Q | Answer | Mark | Comments |
|----|---|------|----------|
| 13 | Alternative method 1 | | |
| | $\frac{206}{770} \times 60$ or $\frac{50}{770} \times 60$ or 16.05(...) or 3.89(6) or 16 or 4 | M1 | |
| | their 16 – their 4 or their 16.05(..)- their 3.89(6..) | M1 | |
| | 12 | A1 | |
| | Alternative method 2 | | |
| | 206 – 50 or 156 | M1 | |
| | $\frac{156}{770} \times 60$ or 12.1(..) | M1 | |
| | 12 | A1 | |

| Q | Answer | Mark | Comments |
|--------------|---|------|-------------------------------------|
| 14(a) | Alternative method 1 | | |
| | 4000 × (£)15 or (£) 60 000 | M1 | |
| | 125 or 1.25 seen | M1 | |
| | 60 000 ÷ 1.25 = 48 000 | A1 | oe |
| | Alternative method 2 | | |
| | 125 or 1.25 seen | M1 | oe |
| | $\frac{15 \times 100}{125}$ or $15 \div 1.25$ or 12 | M1 | |
| | their $12 \times 4000 = 48\ 000$ | A1 | |
| 14(b) | Alternative method 1 | | |
| | 48 000 × 1.2 or 57 600 | M1 | |
| | $x \times 5$ or $(4000 - x) \times 15$ | M1 | where x is the number damaged |
| | $5x + (4000 - x) \times 15 = 57\ 600$ | M1 | Any correct equation |
| | $10x = 2400$ | M1 | |
| | 240 | A1 | |
| | Alternative method 2 | | |
| | 48 000 × 1.2 or 57 600 | M1 | |
| | $x \times 15$ or $(4000 - x) \times 5$ | M1 | where x is the number not damaged |
| | $15x + (4000 - x) \times 5 = 57\ 600$ | M1 | Any correct equation |
| | $10x = 37\ 600$ | M1 | or 3760 not damaged |
| | 240 | A1 | |

| Q | Answer | Mark | Comments |
|--------------|--|------|---------------------------------------|
| 14(b) | Alternative method 3 (Equation based on profit) | | |
| | 48 000 × 0.2 or 9600 | M1 | |
| | $x \times -7$ or $(4000 - x) \times 3$ | M1 | where x is the number damaged oe |
| | $-7x + (4000 - x) \times 3 = 9600$ | M1 | Any correct equation |
| | $10x = 2400$ | M1 | |
| | 240 | A1 | |
| | Alternative method 4 | | |
| | 48 000 × 1.2 or 57 600 | M1 | |
| | 60000 – 57600 or 2400 | M1 | |
| | (Difference in price = £)10 | M1 | |
| | $2400 \div 10$ | M1 | |
| | 240 | A1 | |

| Q | Answer | Mark | Comments | |
|---------|---|-------|---|--|
| 15(a) | $40 \div 5$ or $72 \div 10$ or $102 \div 30$ | M1 | May be implied by one correct height | |
| | 8 and 7.2 and 3.4 | A1 | | |
| | All bars drawn correct height and width | A1 | | |
| 15(b) | 10×5.4 or 20×5.2 or 5×11 | M1 | Implied by one correct value | |
| | 54, 104, 55 | A2 | A1 for 2 correct values | |
| 15(c) | Alternative method 1 | | | |
| | $\frac{25}{30} \times 102$ or 17 seen | M1 | oe | |
| | 85 | A1 | | |
| | Alternative method 2 | | | |
| | 25 x their 3.4 | M1 | | |
| | 85 | A1 ft | Ft their frequency density | |
| | | | | |
| 16(a) | $5x + 2.5y \geq 75$ | B1 | | |
| 16(bi) | $2x + y \geq 30$ drawn on graph | B1 | | |
| | Correct region shown clearly. | B1 | Accept shaded in or shaded out. | |
| 16(bii) | Trial of any integer point at or near any vertex | M1 | (12,24) => £120 (18,18) => £135 (8, 15) => £77.5(0) (10, 10) => £75 (17,18) => £130 (17,19) => £132.50 | |
| | Trial of (17,19) | M1 | This implies first M1 also | |
| | £132.50 | A1 | SC2 for £135 | |
| | Additional guidance | | Mark | |
| | SC2 for 135 is for those who do not realise that the line $y = x$ is dotted(the number of children must be more than the number of adults) and therefore values on the line cannot be included | | | |