## AQA <br> E

Please write clearly in block capitals.

Centre number


Candidate number


Surname $\qquad$
Forename(s)
Candidate signature
I declare this is my own work.

## GCSE

MATHEMATICS

## Higher Tier

## Paper 3 Calculator

Monday 8 June 2020
Morning
Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments.


## Instructions



- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.


## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80 .
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

| For Examiner's Use |  |
| :---: | :---: |
| Pages | Mark |
| $2-3$ |  |
| $4-5$ |  |
| $6-7$ |  |
| $8-9$ |  |
| $10-11$ |  |
| $12-13$ |  |
| $14-15$ |  |
| $16-17$ |  |
| $18-19$ |  |
| $20-21$ |  |
| $22-23$ |  |
| $24-25$ |  |
| $26-27$ |  |
| TOTAL |  |

## Advice

In all calculations, show clearly how you work out your answer.

Answer all questions in the spaces provided.

1 What does $A \cup B$ represent in $P(A \cup B)$ ? Circle your answer.

A or B or both
not $A$ and $\operatorname{not} B$

A but not B
$A$ and $B$

2 Circle the equation of the line that is parallel to $y=\frac{1}{2} x+3$

$$
y=-2 x \quad y=2 x \quad y=\frac{1}{2} x \quad y=-\frac{1}{2} x
$$

3 Work out 320 as a percentage of 80
Circle your answer.
$300 \%$
400\%
4 A fair coin is spun four times.
Circle the probability of getting four Heads.
$\frac{1}{2}$

5 To the nearest 1000, there are 18000 people at a festival.

5 (a) Write down the minimum possible number of people at the festival.

Answer $\qquad$

5 (b) Write down the maximum possible number of people at the festival.

Answer $\qquad$
$\frac{1}{2}$
16

## Answ

$\qquad$

## Tur over for the next question

$\qquad$
$6 \quad A B C D$ represents the plan of a field.


There is a path across the field that
starts at $B$
is the same distance from $B A$ and $B C$.
Using ruler and compasses, show the position of the path.

7 Use Pythagoras' theorem to work out the value of $x$.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ cm

8 Chris visits a library.
He cycles to the library in half an hour at a speed of 12 miles per hour.
He stays at the library for one hour.
He then cycles home.
The sketch graph represents his visit.

Distance from home (miles)


Work out the speed, in miles per hour, at which Chris cycles home.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ mph
$9 \quad$ These two triangles are similar.
Not drawn
accurately


Work out the value of $a$.
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ cm

10 Expand and simplify fully $\quad 4(2 c+3)-(5 c-1)$
[2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

11 A spinner can land on red, blue or green.
After 350 spins
relative frequency of red $=0.18$
relative frequency of blue $=0.62$
Work out the number of times the spinner landed on green.
$\qquad$

Answer $\qquad$

12 Here is some information about 26 houses.
$a, b$ and $c$ are all different numbers.

| Number of bedrooms | Number of houses |
| :---: | :---: |
| 1 | 7 |
| 2 | $a$ |
| 3 | $b$ |
| 4 | $c$ |
| 5 | 8 |

The median number of bedrooms is 3.5
Work out a possible set of values for $a, b$ and $c$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$a=$ $\qquad$
$b=$ $\qquad$
$c=$ $\qquad$

13 (a) Simplify $\frac{25 a}{8} \times \frac{2 a}{5}$
Give your answer as a single fraction in its simplest form.

## Answer

13 (b) Sofia is trying to simplify $\frac{6 c+10}{2}$
Her method is
divide $6 c$ by 2
then
add 10

Evaluate her method.
[1 mark]
$\qquad$
$\qquad$
$\qquad$

14 A rectangle has length 60 cm and width 40 cm


The length decreases by $15 \%$
The width decreases by $10 \%$
Sue says,
"The perimeter decreases by $25 \%$ because $15 \%+10 \%$ is $25 \%$ "
Is she correct?
You must show calculations to support your answer.
$\qquad$
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$15 \quad$ Solve $\quad 4>11-\frac{x}{3}$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer

16 The number of goals scored by 20 players in a season is shown.

| Number of goals | Frequency | Midpoint |  |
| :---: | :---: | :---: | :--- |
| 0 to 4 | 6 |  |  |
| 5 to 9 | 11 |  |  |
| 10 to 14 | 3 |  |  |
| Total $=20$ |  |  |  |

Work out an estimate of the mean number of goals per player.
Give your answer as a decimal.
[3 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

17 Here are two rectangles.
Not drawn accurately


The area of the shaded rectangle is $\frac{1}{4}$ the area of the large rectangle. Work out the value of $x$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

18 The pressure in a tyre is 30 pounds per square inch.
Convert the pressure into kilograms per square centimetre.
Use 1 pound $=0.45$ kilograms
and
1 inch $=2.54$ centimetres

| Use | 1 pound $=0.45$ kilograms |
| :--- | :--- |
| and |  |
|  | 1 inch $=2.54$ centimetres |

$\qquad$
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$\qquad$

Answer $\qquad$ $\mathrm{kg} / \mathrm{cm}^{2}$

19 The sketch shows the lines $x=1$ and $y=-3$


Which pair of inequalities describes the shaded region? Tick one box.


$$
x<1 \text { and } y<-3
$$



$$
x<1 \text { and } y>-3
$$


$x>1$ and $y>-3$


$$
x>1 \text { and } y<-3
$$

## Turn over for the next question

20 Amari and Ben each play a game.
20 (a) Here is some information about Amari's scores.

## Lowest 12

Highest 20
Lower quartile 13
Upper quartile 19
Median 17

Draw a box plot to represent his scores.

Amari


20 (b) This box plot represents Ben's scores.
Ben


Who had more consistent scores, Amari or Ben?
Work out the interquartile ranges to support your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
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$\qquad$

Turn over for the next question

21 (a) $A$ and $B$ are points on a circle.
$P A$ and $P B$ are tangents.


Not drawn accurately

Work out the size of angle $A P B$.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$ degrees

21 (b) $C, D$ and $E$ are points on a different circle.


Not drawn accurately

Is $X$ the centre of the circle?
Tick a box.


Show working to support your answer.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Turn over for the next question

22 Visitors to a museum buy a child ticket or an adult ticket.
Here is some information about two groups of visitors.

| Group $\mathbf{X}$ | 250 visitors, including 120 children |
| :--- | :--- |
| Group $\mathbf{Y}$ | number of children : number of adults $=17: 15$ |

One visitor from each group is picked at random.
Is this statement correct?

Probability of picking two children > probability of picking two adults

You must show your working.
$\qquad$
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23 In triangle JKL
$M$ is the midpoint of $J K$
$J N: N L=3: 2$
$\overrightarrow{K L}=7 \mathbf{a} \quad \overrightarrow{N L}=4 \mathbf{b}$


Not drawn accurately

Work out $\overrightarrow{J M}$ in terms of $\mathbf{a}$ and $\mathbf{b}$.
Give your answer in its simplest form.
$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$
$24 \quad A$ and $B$ are points on a curve.
$A$ is $(2,7) \quad B$ is $(12,0)$


24 (a) Work out the instantaneous rate of change of $y$ with respect to $x$ at point $A$.
[2 marks]
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Answer $\qquad$

24 (b) The average rate of change of $y$ with respect to $x$ between points $A$ and $B$ is worked out. Which statement is correct?

Tick one box.


It is positive.


It is zero.


It is negative.


You cannot tell if it is positive or negative.

25 The equation of a circle is $x^{2}+y^{2}=9$
Work out the length of the diameter.
Circle your answer.

$$
26 \quad \text { Prove algebraically that } \quad 3.4 \dot{7}=\frac{313}{90}
$$

$\qquad$
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27 The equation of a curve is $y=(x-1)^{2}-6$
Circle the coordinates of the turning point.
$(-1,-6)$
$(1,6)$
$(-1,6)$
(1, -6)

28 Line A has equation $y=4 x-1$
Line $B$ is
perpendicular to line A
and
passes through the point $(8,5)$
Work out the coordinates of the point where line B intersects the $x$-axis.
$\qquad$
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$\qquad$

Answer ( $\qquad$ , $\qquad$ )

## Turn over for the next question

Whe

29 A shape is made by joining triangle $A B C$ to a semicircle with diameter $A C$.

Not drawn
 accurately

Work out the total area of the shape.
$\qquad$
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Answer $\qquad$ $\mathrm{cm}^{2}$
$30 \quad \mathrm{f}(x)=\frac{1}{2} x \quad \mathrm{~g}(x)=x-x^{2}$
Solve $\quad \mathrm{f}^{-1}(x)=\mathrm{gf}(x)$
$\qquad$
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Answer $\qquad$



| Question number | Additional page, if required. <br> Write the question numbers in the left-hand margin. |
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## There are no questions printed on this page

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