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# GCSE MATHEMATICS

**H**

Higher Tier      Unit 3      Geometry and Algebra

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Tuesday 8 November 2016

Morning

Time allowed: 1 hour 30 minutes

## Materials

For this paper you must have:

- a calculator
- mathematical instruments.



## Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work that you do not want to be marked.
- If your calculator does not have a  $\pi$  button, take the value of  $\pi$  to be 3.14 unless another value is given in the question.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- Quality of written communication is specifically assessed in Questions 1 and 5.  
These questions are indicated with an asterisk (\*).
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

## Advice

- In all calculations, show clearly how you work out your answer.



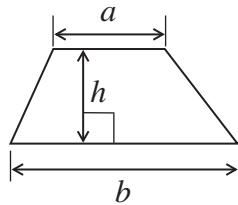
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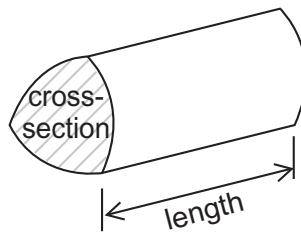
**43603H**

### Formulae Sheet: Higher Tier

**Area of trapezium** =  $\frac{1}{2} (a + b)h$

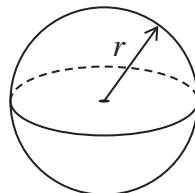


**Volume of prism** = area of cross-section  $\times$  length



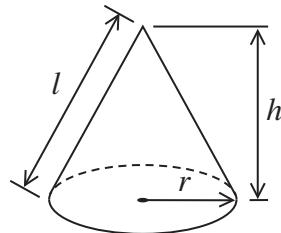
**Volume of sphere** =  $\frac{4}{3} \pi r^3$

**Surface area of sphere** =  $4\pi r^2$



**Volume of cone** =  $\frac{1}{3} \pi r^2 h$

**Curved surface area of cone** =  $\pi r l$

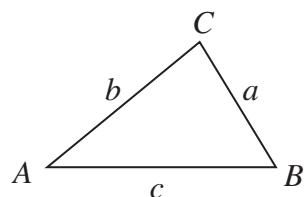


In any triangle  $ABC$

**Area of triangle** =  $\frac{1}{2} ab \sin C$

**Sine rule**  $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$

**Cosine rule**  $a^2 = b^2 + c^2 - 2bc \cos A$



### The Quadratic Equation

The solutions of  $ax^2 + bx + c = 0$ , where  $a \neq 0$ , are given by

$$x = \frac{-b \pm \sqrt{(b^2 - 4ac)}}{2a}$$



Answer **all** questions in the spaces provided.

- \*1 The same type of shirt is sold in two shops.

**Shop A**



£19.90

Buy one  
get second for half price

**Shop B**



£18

Get a 15% discount  
when you buy two

Which shop is cheaper for buying **two** of these shirts?

You **must** show your working.

[5 marks]

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Answer \_\_\_\_\_

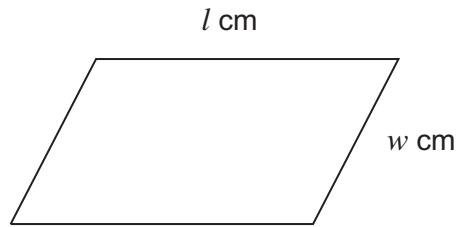
5

Turn over ►



0 3

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**2 (a)**

The perimeter of the parallelogram is  $P$  cm

Circle the correct formula.

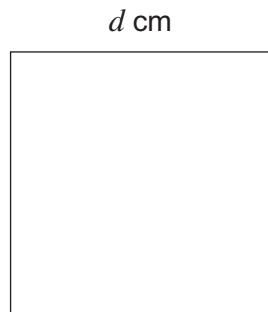
**[1 mark]**

$$P = l + w$$

$$P = lw$$

$$P = 2(l + w)$$

$$P = 2lw$$

**2 (b)**

The area of the square is  $A$   $\text{cm}^2$

Circle the correct formula.

**[1 mark]**

$$A = 2d$$

$$A = 4d$$

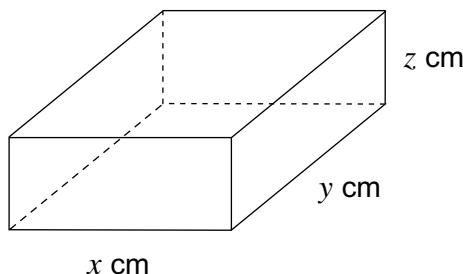
$$A = \sqrt{d}$$

$$A = d^2$$



0 4

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**2 (c)**

The surface area of the cuboid is  $S \text{ cm}^2$

Circle the correct formula.

**[1 mark]**

$$S = xyz$$

$$S = (xyz)^2$$

$$S = 6xyz$$

$$S = 2(xy + xz + yz)$$

**2 (d)** The surface area of a **cube** is  $150 \text{ cm}^2$

Work out the volume of the cube.

**[4 marks]**

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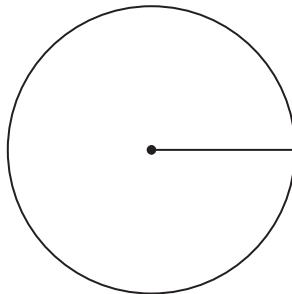
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Answer \_\_\_\_\_  $\text{cm}^3$



- 3 (a) The radius of this circle is 2.5 cm

Not drawn accurately



Work out the area.

Give your answer to 1 significant figure.

[3 marks]

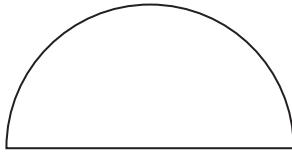
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Answer \_\_\_\_\_  $\text{cm}^2$

- 3 (b) The diameter of this semicircle is 16 cm

Not drawn accurately



Work out the perimeter of the semicircle.

[3 marks]

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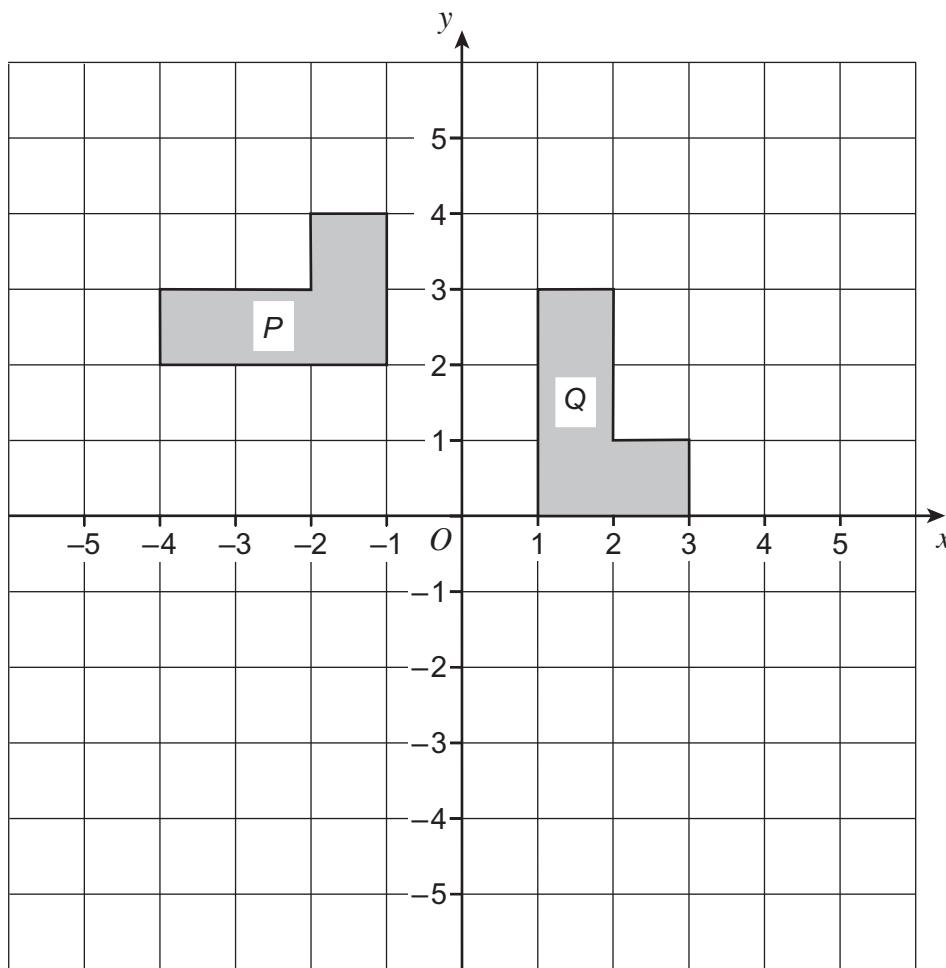
Answer \_\_\_\_\_  $\text{cm}$



0 6

- 4 (a) Describe fully the **single** transformation that maps shape  $P$  to shape  $Q$ .

[3 marks]



- 4 (b) On the grid, translate shape  $Q$  by vector  $\begin{pmatrix} 1 \\ -5 \end{pmatrix}$

[2 marks]

11

Turn over ►



0 7

WMP/Nov16/43603H

- \*5 Use trial and improvement to find a positive solution to  $x^3 - 10x = 6$   
Give your answer to 1 decimal place.

[4 marks]

$x$	$x^3 - 10x$	Comment
4	24	Too big

$x =$  \_\_\_\_\_



- 6 Ali is going to drive 210 miles.

He has 27 **litres** of petrol in his car.  
His car travels 36 miles for each **gallon** of petrol.

Does he have enough petrol for the journey?  
You **must** show your working.

[4 marks]

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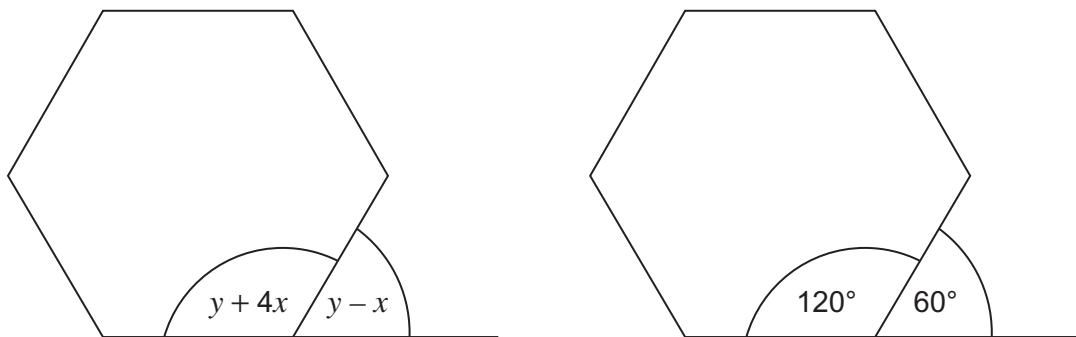
Answer \_\_\_\_\_

**Turn over for the next question**



**7**

The diagram shows two regular hexagons with the base lines extended.



Work out the values of  $x$  and  $y$ .

[5 marks]

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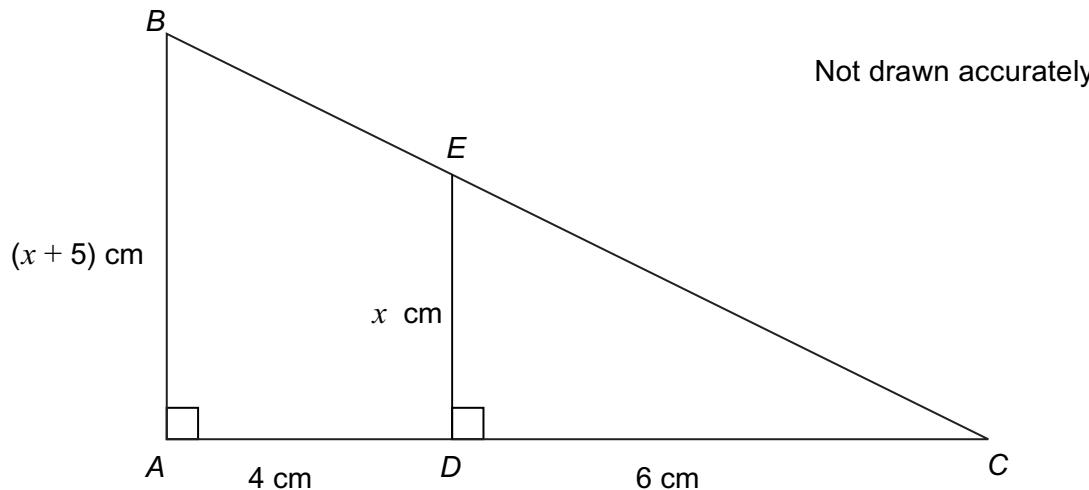
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$$x = \underline{\hspace{2cm}} \text{ degrees}$$

$$y = \underline{\hspace{2cm}} \text{ degrees}$$



**8***ABC* and *DEC* are similar triangles.Work out the value of  $x$ .**[4 marks]**


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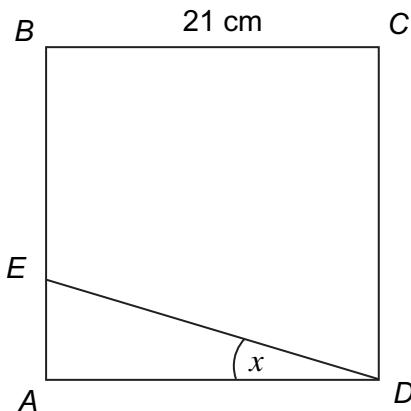
Answer \_\_\_\_\_ cm

**9****Turn over ►**

1 1

**9**

ABCD is a square.



Not drawn accurately

$$AE = \frac{2}{5} EB$$

Work out the size of angle  $x$ .

[4 marks]

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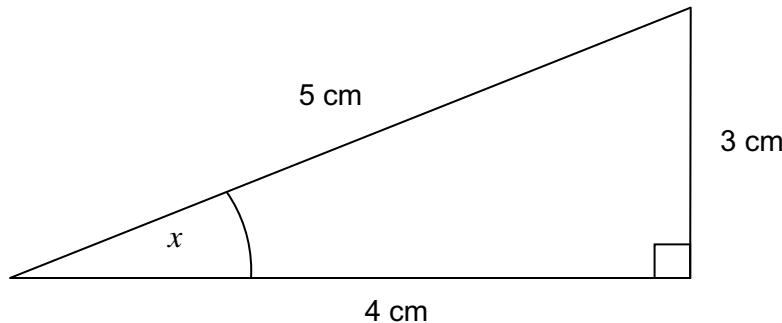
Answer \_\_\_\_\_ degrees



1 2

**10 (a)**

Not drawn accurately

Circle the value of  $\sin x$ .**[1 mark]**

$\frac{3}{5}$

$\frac{3}{4}$

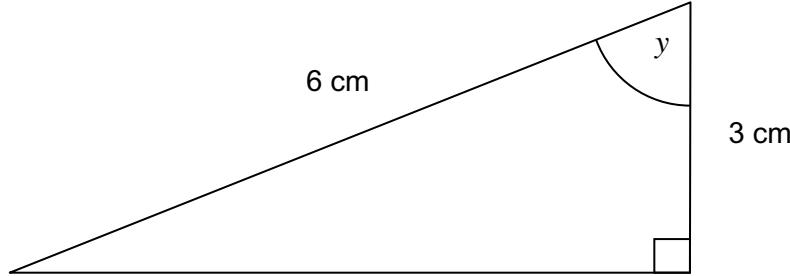
$\frac{4}{5}$

$\frac{4}{3}$

$\frac{5}{3}$

**10 (b)**

Not drawn accurately

Circle the size of angle  $y$ .**[1 mark]**

$30^\circ$

$36^\circ$

$45^\circ$

$50^\circ$

$60^\circ$

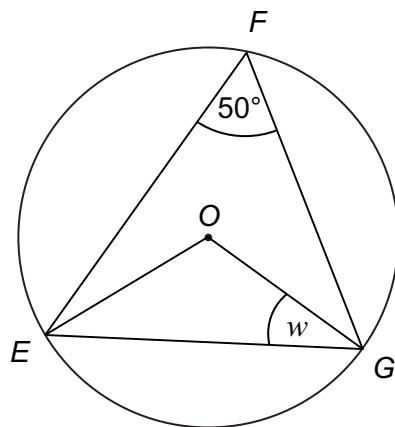
**6**

**Turn over ►**

1 3

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- 11 (a)**  $E, F$  and  $G$  are points on a circle, centre  $O$ .



Not drawn accurately

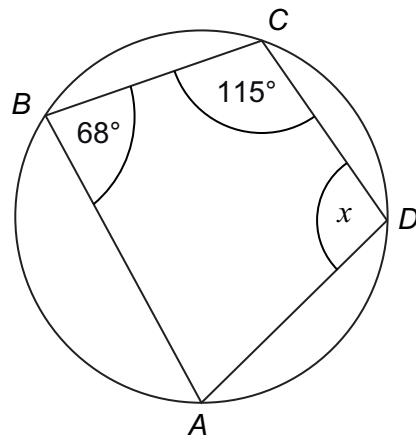
Work out the size of angle  $w$ .

[2 marks]

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Answer \_\_\_\_\_ degrees

- 11 (b)**  $A, B, C$  and  $D$  are points on the circumference of the circle.



Not drawn accurately

Work out the size of angle  $x$ .  
Give a reason for your answer.

[2 marks]

Answer \_\_\_\_\_ degrees

Reason \_\_\_\_\_

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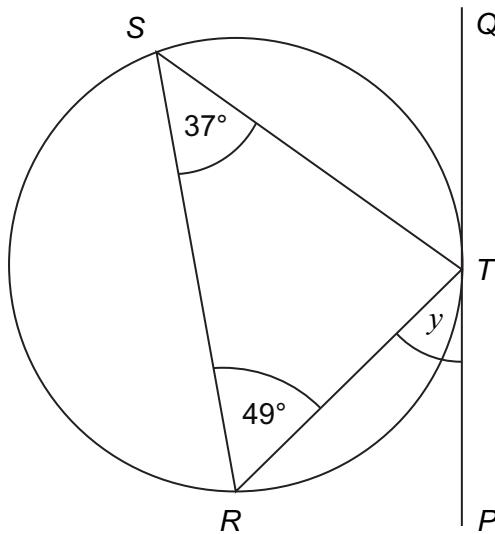


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- 11 (c)  $PTQ$  is a tangent to the circle.  
 $R$ ,  $S$  and  $T$  are points on the circle.

Not drawn accurately



Write down the size of angle  $y$ .  
Give a reason for your answer.

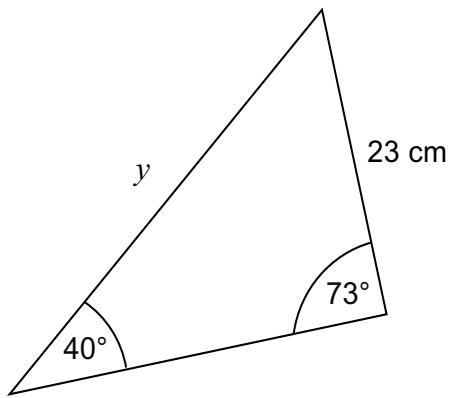
[2 marks]

Answer \_\_\_\_\_ degrees

Reason \_\_\_\_\_  
\_\_\_\_\_

Turn over for the next question



**12**Work out length  $y$ .Not drawn  
accurately**[3 marks]**

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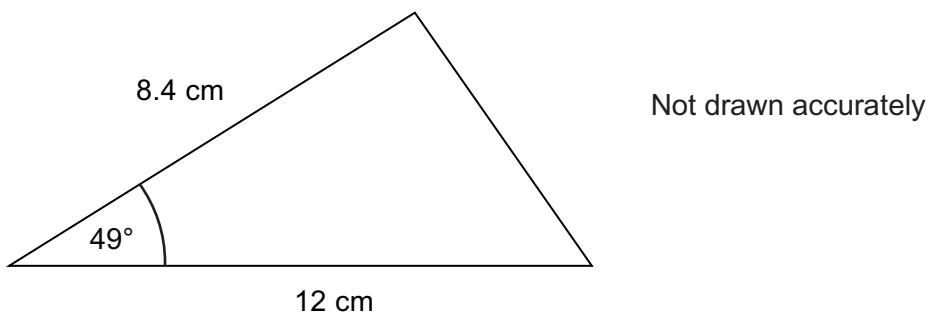
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Answer \_\_\_\_\_ cm



**13**

Work out the area of the triangle.

**[2 marks]**Answer \_\_\_\_\_  $\text{cm}^2$ **14**Solve  $2x^2 + 3x - 6 = 0$ 

Give your answers to 2 decimal places.

**[3 marks]**

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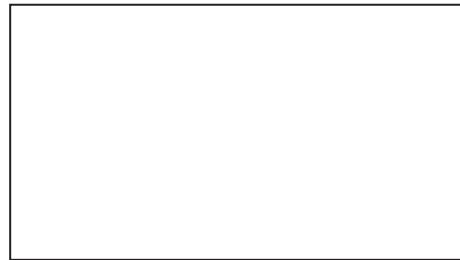
Answer \_\_\_\_\_ and \_\_\_\_\_

8

**Turn over ►**

**15**The area of this rectangle is  $28 \text{ cm}^2$ 

Not drawn accurately

 $(6x - 1) \text{ cm}$ 

Work out the perimeter of the rectangle.

**[7 marks]**

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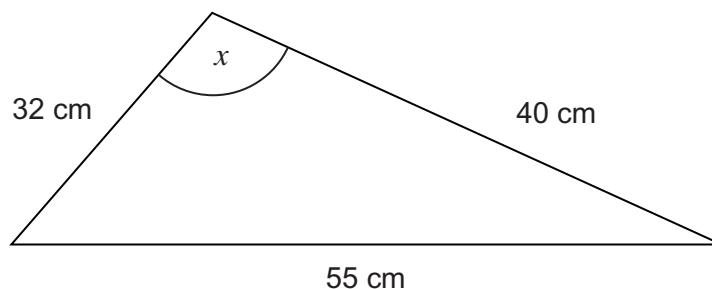
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Answer \_\_\_\_\_ cm



**16**Work out the size of angle  $x$ .Not drawn  
accurately**[3 marks]**

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Answer \_\_\_\_\_ degrees

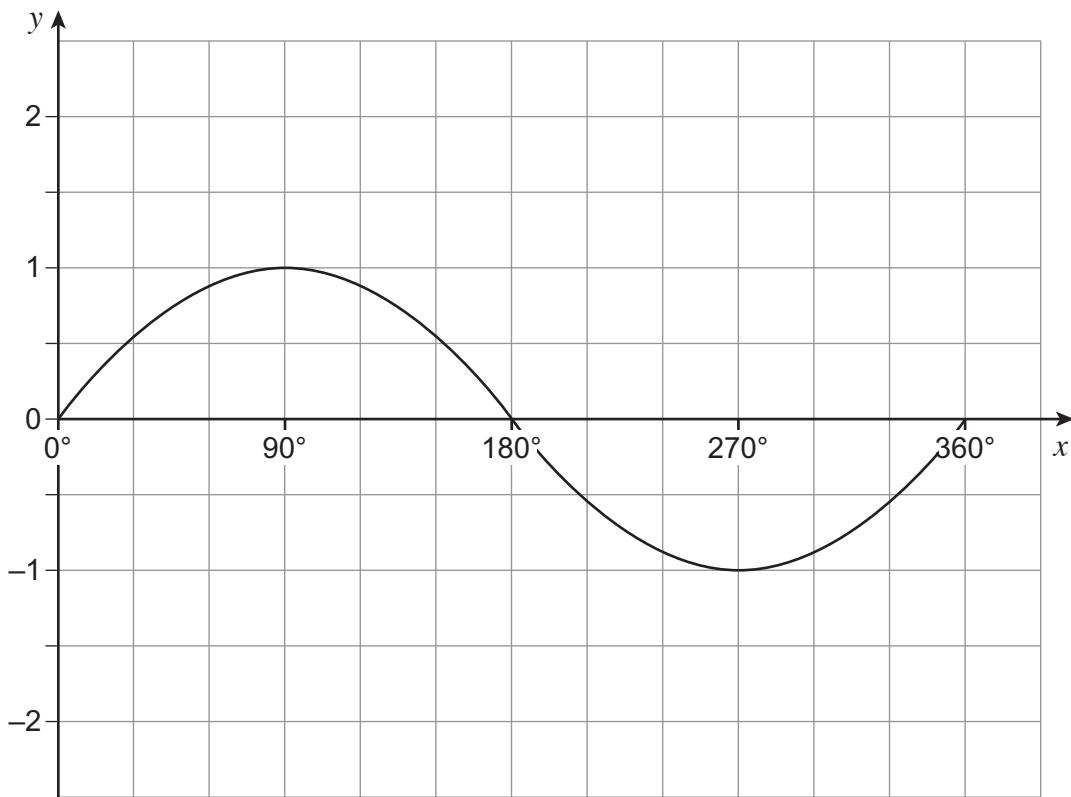
**Turn over for the next question****10****Turn over ►**

1 9

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17

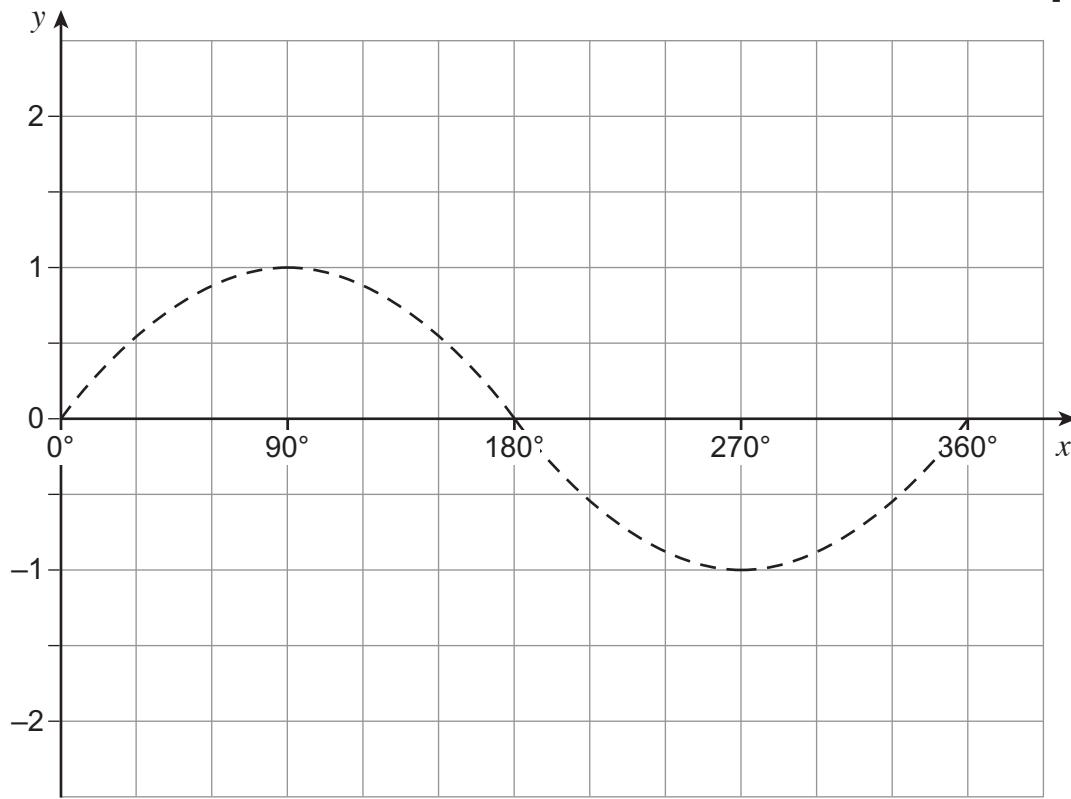
The graph of  $y = \sin x$  for  $0^\circ \leq x \leq 360^\circ$  is shown.



17 (a) On the grid below, draw the graph of  $y = 1 + \sin x$  for  $0^\circ \leq x \leq 360^\circ$

The graph of  $y = \sin x$  is shown to help you.

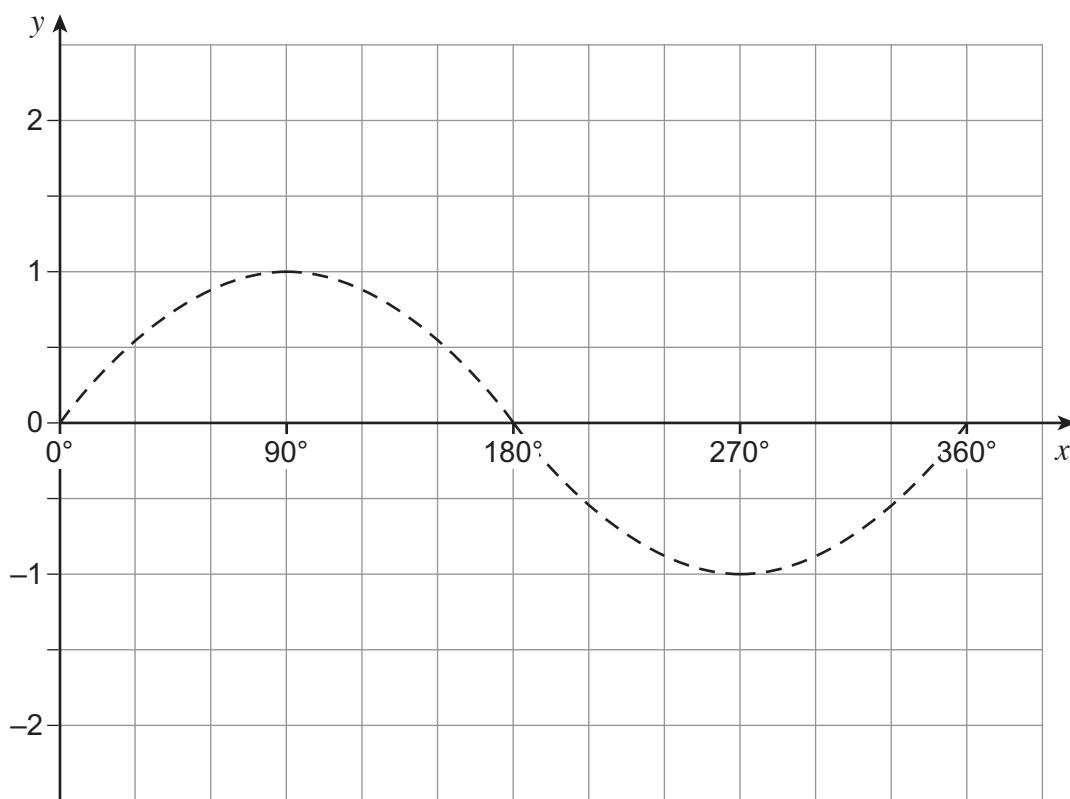
[1 mark]



- 17 (b) On the grid below, draw the graph of  $y = \sin(x + 90^\circ)$  for  $0^\circ \leq x \leq 360^\circ$

The graph of  $y = \sin x$  is shown to help you.

[1 mark]



Turn over for the next question

2

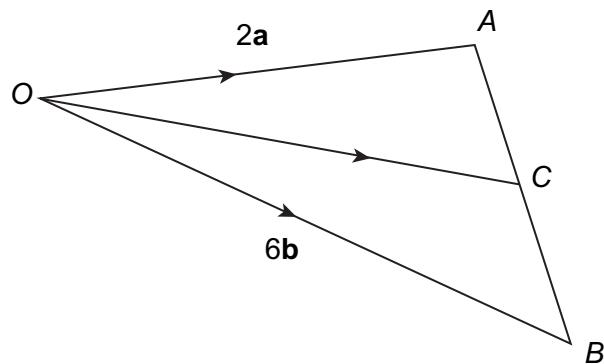
Turn over ►



2 1

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18

 $C$  is the midpoint of  $AB$ .

$$\overrightarrow{OA} = 2\mathbf{a}$$

$$\overrightarrow{OB} = 6\mathbf{b}$$

$\overrightarrow{OC}$   
Work out  $OC$  in terms of  $\mathbf{a}$  and  $\mathbf{b}$ .  
Simplify your answer as far as possible.

[4 marks]

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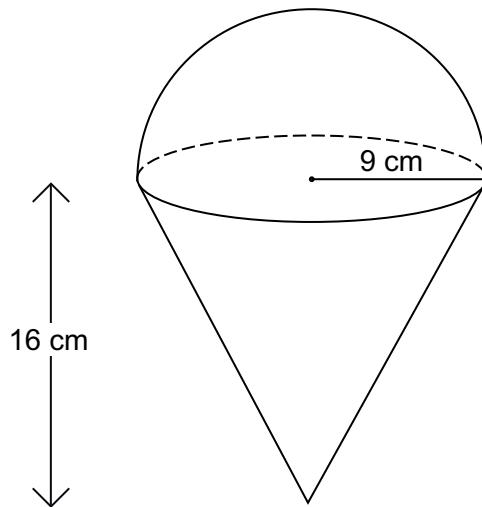
Answer \_\_\_\_\_



2 2

**19**

A hemisphere and a cone each have radius 9 cm  
They are joined together to make a toy.



Work out the total volume of the toy.

**[4 marks]**

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Answer \_\_\_\_\_  $\text{cm}^3$

**END OF QUESTIONS**

**8**



2 3

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ANSWER IN THE SPACES PROVIDED**

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2 4

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