

AQA Qualifications

# GCSE

## **Mathematics**

Unit 3: Foundation 43603F Mark scheme

43603F June 2016

Version: 1.0 Final

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from aqa.org.uk

### **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

M	Method marks are awarded for a correct method which could lead
	to a correct answer.

- **M dep** A method mark dependent on a previous method mark being awarded.
- A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- **B** Marks awarded independent of method.
- **B dep** A mark that can only be awarded if a previous independent mark has been awarded.
- **ft** Follow through marks. Marks awarded following a mistake in an earlier step.
- SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as  $\frac{1}{2}$
- [a, b] Accept values between a and b inclusive.
- **[a, b)** Accept values  $a \le \text{value} < b$
- **3.14...** Accept answers which begin 3.14 eg 3.14, 3.142, 3.1416

#### Examiners should consistently apply the following principles

#### **Diagrams**

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

#### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

#### Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

#### Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

#### Continental notation

Accept a comma used instead of a decimal point (for example, in measurements or currency), provided that it is clear to the examiner that the candidate intended it to be a decimal point.

Q	Answer	Mark	Comments		
· ·	Allowel	IVICITA	Comments		
	[9.9, 10.1]	B1	oe		
1(a)	Ad	ditional G	Guidance		
	6 + 8 + [9.9, 10.1]		oe		
	or 6 + 8 + their [9.9, 10.1]	M1	60 + 80 + [99, 101]		
	or or or anom tors, remain		60 + 80 + their [99, 101]		
1(b)	[23.9, 24.1]	A1ft	[239 mm, 241 mm]		
	Ad	ditional G	Guidance		
	$6 \times 8 \div 2 = 24$	M0A0			
	If length of hypotenuse seen on diagram follow through for their total				
		T			
2(a)	В	B1			
		Т	I		
2(b)	C and E	B1			
	T		I		
2(c)	A and D	B1			
			Any order		
	C and E	B2	B1 for 1 correct		
3(a)			or for 1 correct and 1 incorrect		
σ(u)			or for 2 correct and 1 incorrect		
	Ad	ditional G	<del>S</del> uidance		

Q	Answer	Mark	Comments		
	1	I			
3(b)	B, C and E	B2	Any order B1 for 2 correct or for 2 correct and 1 incorrect or for 3 correct and 1 incorrect		
	Ac	dditional (	Guidance		
<b>2</b> ( )	A	B1			
3(c)	Additional Guidance				
4(a)	Sevilla	B1			
4(b)	Barcelona	B1			
	[4.9, 5.1]	B1			
	their [4.9, 5.1] × 125	M1			
4(c)	[612.5, 637.5]	A1ft	ft B0 M1		
	Ac	dditional (	Guidance		

Q	Answer	Mark	Comments	
	350	B1		
5(a)	Ac	ditional G	Guidance	
5(b)	States or implies 1 kg = 1000 g or 0.6 kg = 600 g	M1		
	Correct combination for 600 g	A1	oe eg 400 + 200 300 + 300 combination must be in grams	
	Additional Guidance			
	200 + 200 + 200 = 606 is a slip (answer not required as given)			M1A1
		ı	,	
6(a)	$\frac{1}{8}$ and $\frac{2}{16}$	B2	B1 for 1 correct or for 1 correct and 1 incorrect or for 2 correct and 1 incorrect SC1 for $\frac{1}{7}$ and $\frac{2}{14}$ or $\frac{7}{8}$ and	14

Q	Answer	Mark	Comments	
6(b)	8 squares shaded seen or implied or 8 squares unshaded seen or implied or $\frac{16}{32}$ or $\frac{8}{16}$ or $\frac{4}{8}$ or $\frac{1}{2}$	M1	oe	
	50 (%)	A1		
	Additional Guidance			
	$\frac{12}{24} = 50 \text{ (\%) or } \frac{6}{12} = 50 \text{ (\%) is from incorrect working}$			

7(a)	4 × 45.5(0) or 182	M1		
	their 182 ÷ 26	M1dep		
	7	A1		
	Additional Guidance			
	26 x 7 = 182 (embedded answer)			M1M1A0

Q	Answer	Mark	Comments	
	A correctly evaluated trial adding prices of 5 tins	g the M1		
	3 (5-litre tins)			
	and	A1		
	2 (10-litre tins)			
	Additional Guidance			
7(b)	Note:			
	5 × 26 = 130			
	4 × 26 + 45.5 or 104 + 45			
	3 × 26 + 2 × 45.5 or 78 + 91 =			
	2 × 26 + 3 × 45.5 or 52 + 136			
	26 + 4 × 45.5 or 26 + 182	2 = 208		
	5 × 45.5 = 227.5			

8(a)	(1, 1)	B2	B1 for x-coordinate 1 or y-coordinate 1 or $AC = 6$ or $\frac{1}{2}AC = 3$
	Ad	ditional G	Guidance
	Check diagram for working		

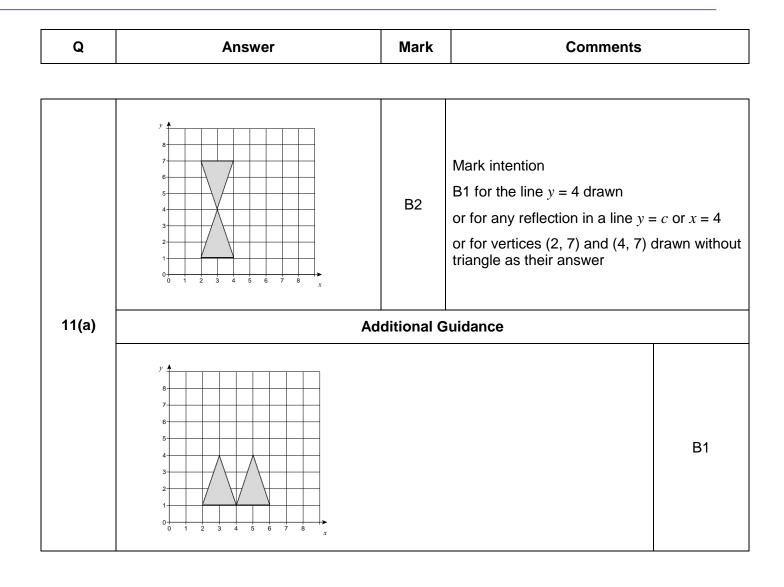
Q	Answer	Mark	Comments	
			B1 for <i>x</i> -coordinate 4	
			or y-coordinate –7	
	(4, -7)	B2	or <i>BD</i> = 16	
8(b)			or $\frac{1}{2}BD = 8$	
	Additional Guidance			
	Check diagram for working			

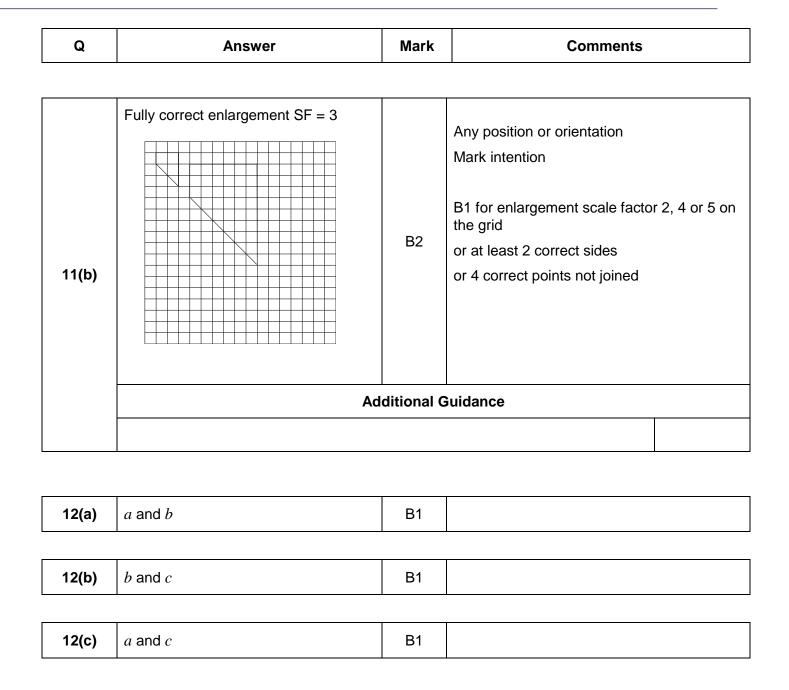
	6 × 25 × 10 or 1500	M1	
	their 1500 ÷ 30	M1dep	Fully correct method
9	50	A1	Do not ignore fw
	Additional Guidance		

10(a)	Two correct points plotted eg (10, 12) and (20, 24)  Straight ruled line through their correct points	M1 A1	eg (5, 6) and (10, 12)  Ignore incorrect points  ± ½ square tolerance  ± ½ square tolerance	
	Additional Guidance			
	If line goes through (0, 0) this can be accepted as a correct point			

Q	Answer	Mark	Comments
10(b)	15	B1	

	12 ÷ 10 or 1.2 or 10 ÷ 12 or 0.83() or 480 (square yards)	M1	Scale factor 1.2 seen or implied or 10 to 400 is area factor 40 seen or implied
10(c)	$25 \times 480$ or $25 \times 400 \times 1.2$ or $25 \times 400 \div 0.83()$	M1dep	oe eg 25 × 40 × 12
	12 000	A1	Accept [12 000, 12 050] SC1 for 10 000
	Additional Guidance		Guidance
	25 × 480		M1M1





Q	Answer	Mark	Comments	
	Alternative method 1			
	A pair of intersecting arcs of radii 4 cm	M1		
	A pair of intersecting arcs of radii 8 cm	M1		
	Fully correct kite drawn with all arcs shown	A1	SC1 for a complete kite within	tolerance
	Alternative method 2 (perper	ndicular bis	sector)	
13	Two pairs of intersecting arcs of equal radii greater than 3 cm	M1		
	Perpendicular bisector constructed	M1dep		
	Fully correct kite drawn with at least one arc of radius 4 cm and one arc of radius 8 cm	A1	SC1 for a complete kite within	tolerance
	Additional Guidance			
	Kite may be drawn inverted			
	52 + 75 + 59 or 186	M1	oe	
	or 360 – 52 – 75 – 59	IVII	x + 52 + 75 + 59 = 360	
	174	A1		
14(a)	Ad	ditional G	Guidance	
	52 + 75 + 59 may be embedded within a	an incorred	ct calculation	M1

360 - 52 + 75 + 59 = 174 (recovered)

360 - 52 + 75 + 59 (= 442)

M1A1

M0A0

Q	Answer	Mark	Comments	
	AED = 100 or $E = 100or ADE = 40 or D = 40or DAE = 40 or A = 40$	B1	May be on diagram in the corre	ect place
	(BAD =) 180 – 117 or 63 seen or implied	M1	oe May be on diagram in the corre	ect place
14(b)	103	A1		
14(b)	Additional Guidance			
	Beware of contradictions between diagr			
BAD shown as 63 on diagram in correct position  180 – 117 with nothing marked on diagram and no contradiction			M1	
		o contradiction	M1	
	180 – 117 = 63, 63 only marked at <i>C</i> on	MO		
	Condone assumption for symmetry of tr	apezium (	360 – 2 × 117) ÷ 2	M1

Q	Ans	swer	Mark	Comments	
	Alternative method 1				
	$\frac{15}{100} \times 49.8(0)$ or 7.47	49.8(0) ÷ 5 or 9.96	M1	oe 0.85 seen	
15 Alt 1 of 2	49.8(0) – their 7.47 or 42.33	$\frac{15}{100}$ × their 9.96 or 1.49(4)	M1dep	oe 49.8(0) × 0.85 or 42.33	
1012	their 42.33 ÷ 5 or their 9.96 – their 1.49 or 8.466 or 8.46 or 8.47		M1dep		
	8.466 or 8.46 or 8.47 and 5 litres		Q1ft	Strand (iii) ft only for M1M1M0	

Q	Ans	swer	Mark	Comments	
	Alternative method 2				
	$\frac{15}{100} \times 49.8(0)$ or 7.47	49.8(0) ÷ 5 or 9.96	M1	oe 8.75 × 5 or 43.75 or 1 ÷ 8.75 or 0.114 or 0.11	
	49.8(0) – their 7.47 or 42.33	$\frac{15}{100}$ × their 9.96 or 1.49(4)	M1dep	ое	
15 Alt 2 of 2	49.8(0) – their 7.47 or 42.33 and 43.75	8.75 + their 1.49(4) or 10.24(4)	M1dep	1 ÷ 8.75 or 0.114 or 0.11 and 5 ÷ their 42.33 or 0.118	or 0.12
	42.33 and 43.75 and 5 litres	9.96 and 10.24(4) and 5 litres	Q1ft	0.114 and 0.118 and 5 litres or 0.11 and 0.12 and 5 litres Strand (iii) ft only for M1M1M0	es
	Additional Guidance				
	Allow £49.80 or £4	2.33 or large can or s	second car	n or B for Q mark	
	Do not accept £50	for £49.80 unless red	covered		

Q	Answer	Mark	Comments
	95 ÷ 38 or 2.5(0)	M1	oe
	7 + their 2.5(0) or 9.5(0) or 2 hours 30 minutes seen	M1dep	oe
		ivirdep	Allow 2.30 or 2:30
16	9.30 (am) or 0930	A1	oe
	Ad	ditional G	Guidance
	Answer 9 hours 30 minutes		M1M1A0
	9.30 pm or 2130	M1M1A0	

			B1 for 1 correct
17(a)	$c^2 = a^2 + b^2$ and $c = \sqrt{a^2 + b^2}$	B2	or 1 correct and 1 incorrect
			or 2 correct and 1 incorrect

Q	Answer	Mark	Comments		
	22 <sup>2</sup> and 8 <sup>2</sup> seen or 484 and 64 or 420	M1	oe		
17(b)	$\sqrt{22^2 - 8^2}$ or $\sqrt{484 - 64}$ or $\sqrt{420}$ or $2\sqrt{105}$	M1dep			
	20.4(9)	A1			
	20.5	B1ft	ft any 2 dp or better SC2 for final answer of 23.4 only incorrect use of Pythagoras' theo		
	Additional Guidance				
	20.5 on its own			4 marks	
	Trigonometry method could gain marks: M1 for gaining an equation in terms of y M1dep for full method that would lead to an answer of 20.4(9)				

Q	Answer	Mark	Comments
	Alternative method 1		
	4x + 10 + 6x - 15 + 60 = 180 or $4x + 10 + 6x - 15 = 120$	M1	oe
	(x =)12.5	A1	oe
	4 × their 12.5 + 10 or 6 × their 12.5 – 15	M1dep	Dependent on M1
18 Alt	60	A1	
1 of 4	4 × 12.5 + 10 = 60 and 6 × 12.5 – 15 = 60		
	or $4 \times 12.5 + 10 = 60$ and $180 - 60 - 60 = 60$	Q1	Strand (ii)  Accept 60, 60, 60 with 12.5 seen
	or $6 \times 12.5 - 15 = 60$ and $180 - 60 - 60 = 60$		

Q	Answer	Mark	Comments
	Alternative method 2		
	6x - 15 = 4x + 10 or $2x = 25$	M1	oe
	(x =)12.5	A1	oe
	4 × their 12.5 + 10 or 6 × their 12.5 – 15	M1dep	Dependent on M1
18 Alt	60	A1	
2 of 4	$4 \times 12.5 + 10 = 60$ and $6 \times 12.5 - 15 = 60$		
	or $4 \times 12.5 + 10 = 60$ and $180 - 60 - 60 = 60$	Q1	Strand (ii) Accept 60, 60, 60 with 12.5 seen
	or $6 \times 12.5 - 15 = 60$ and $180 - 60 - 60 = 60$		

Q	Answer	Mark	Comments
	Alternative method 3		
	6x - 15 = 60 or $4x + 10 = 60$	M1	oe
	(x =)12.5	A1	oe
	6 × their 12.5 – 15 or 4 × their 12.5 + 10	M1dep	Dependent on M1
18 Alt	60	A1	
3 of 4	$4 \times 12.5 + 10 = 60$ and $6 \times 12.5 - 15 = 60$		
	or $4 \times 12.5 + 10 = 60$ and $180 - 60 - 60 = 60$	Q1	Strand (ii) Accept 60, 60, 60 with 12.5 seen
	or $6 \times 12.5 - 15 = 60$ and $180 - 60 - 60 = 60$		

Q	Answer	Mark	Comments	
	Alternative method 4			
	6x - 15 = 60	M1	oe	
	(x =)12.5	A1	oe	
	4x + 10 = 60	M1	Dependent on M1	
	(x =)12.5	A1	oe	
18 Alt 4 of 4	Valid statement or $4 \times 12.5 + 10 = 60$ and $6 \times 12.5 - 15 = 60$		Strand (ii)	
	or $4 \times 12.5 + 10 = 60$ and $180 - 60 - 60 = 60$ or $6 \times 12.5 - 15 = 60$	Q1	eg Since both <i>x</i> values are 12.5 then all angles are 60 Accept 60, 60, 60 with both A marks awarded	
	and $180 - 60 - 60 = 60$			
	Ad	lditional C	⊥ Guidance	

Q	Answer	Mark	Comments	
19	diameter = 10 (cm) seen or implied or width of rectangle = 10 (cm) seen or implied	B1	May be on diagram	
	radius = 5 (cm) seen or implied	B1dep	May be on diagram	
	10 × 10 or 100 or 20 × 10 or 200	M1	oe	
	$\pi \times 5^2$ or $25\pi$ or $[78.5, 78.6]$ or $79$ or $2 \times \pi \times 5^2$ or $50\pi$ or $[157, 157.2]$ or $158$	M1	oe	
	100 – their $25\pi$ or [21.4, 21.5] or $200 - 2 \times$ their $25\pi$	M1dep	oe Dependent on M1 M1	
	[42.8, 43] or $200 - 50\pi$ or $50(4 - \pi)$ or 42	A1	oe	
	Additional Guidance			
	$200 - 50\pi = 150\pi$ does not score final A mark			5 marks
	20 x 10 or 200 implies			B1M1
	$2 \times \pi \times 5$ implies			B1B1
	$\pi d = 10\pi$ implies			B1
	$10\pi$ on its own			В0