

AQA Qualifications

# GCSE MATHEMATICS

Unit 2 43602H

Mark Scheme

43602H

November 2013

Final version 1.0

Mark schemes are prepared by the Lead Assessment Writer and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all associates participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every associate understands and applies it in the same correct way. As preparation for standardisation each associate analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, associates encounter unusual answers which have not been raised they are required to refer these to the Lead Assessment Writer.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from aqa.org.uk



# **Glossary for Mark Schemes**

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

Μ	Method marks are awarded for a correct method which could lead to a correct answer.
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
В	Marks awarded independent of method.
Q	Marks awarded for Quality of Written Communication
ft	Follow through marks. Marks awarded for correct working following a mistake in an earlier step.
SC	Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
Mdep	A method mark dependent on a previous method mark being awarded.
Bdep	A mark that can only be awarded if a previous independent mark has been awarded.
oe	Or equivalent. Accept answers that are equivalent.
	eg, accept 0.5 as well as $\frac{1}{2}$
[a, b]	Accept values between <i>a</i> and <i>b</i> inclusive.
3.14	Allow answers which begin 3.14 eg 3.14, 3.142, 3.149.
Use of brackets	It is not necessary to see the bracketed work to award the marks.



Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

### Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

#### Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

#### Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

#### Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

#### Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

#### Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

#### Work not replaced

Erased or crossed out work that is still legible should be marked.

#### Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

#### **Premature approximation**

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Q	Answer	Mark	Comments
1	5x - x or $4x$ or $16 + 2$ or $18$	M1	ое
	4x = 18	A1	
	4.5	A1ft	oe ft their rearrangement with one error if M1 awarded

2(a)	300 or 600 or 50 or 100 or 20	M1	
	300 or 600 and 50 or 100 and 20	M1	
	720	A1	SC2 480 SC2 860 SC2 719 SC1 any table value rounded to 1sf SC1 715 SC1 720 without M1 awarded
2(b)	(349 + 349 + 59 + 59 + 39 or 855) – (299 + 299 + 49 + 49 + 19 <b>or</b> 715 <b>or</b> their incorrect total of exact values for July in part(a))	M1	
	140	A1ft	ft 855 – their incorrect total of exact values in part(a)
	Alternative Method		
	$2 \times 50 + 2 \times 10 + 20$ or 350 + 350 + 60 + 60 + 40 – their 720	M1	
	140	A1ft	ft 860 – their 720 from rounding in part(a)



Q	Answer	Mark	Comments
2(a)	$5 \times 5 \times 5$ or $125 \div 5 \div 5 = 5$	B1	
3(a)		Ы	oe Condone $\sqrt[3]{125} = 5$
	or $5^2 = 25$ and $25 \times 5$		
	or $5^2 \times 5$		
	or 5 <sup>3</sup>		
3(b)	a = 4 and $b = 121$	B2	B1
	and		a = 4 and $b = 121$
	a = 25 and $b = 100$		or
	(both in either order)		<i>a</i> = 25 and <i>b</i> = 100
			(either order)
			B1 correct list of square numbers to 100 allow one error or omission
4	Correct method to change $\frac{5}{8}$ and $\frac{2}{3}$	M1	eg $\frac{16}{24}$ , $\frac{15}{24}$ (either way around)
	into fractions with common denominator with at least one correct numerator		24 24
	Correct fractions and No	A1	
	Alternative method 1		
	Correct method to calculate $\frac{5}{8}$ of a	M1	eg $5 \times 40 \div 8$ and $2 \times 40 \div 3$
	chosen value <b>and</b> $\frac{2}{3}$ of the same		or
	3 value		$\frac{5}{8}$ × 40 and $\frac{2}{3}$ × 40
	Correct evaluations and No	A1	

Q	Answer	Mark	Comments
	Alternative method 2		
	Correct method to change $\frac{5}{8}$ and $\frac{2}{3}$ into decimals or percentages	M1	
	$\frac{5}{8} = 0.625 \text{ or } 62.5(\%)$	A1	Correct and consistent decimals or percentages
	$\frac{2}{3} = 0.66(6) \text{ or } 0.67 \text{ or } 66(.6)(\%)$ or 67(%)		
	and No		
5(a)	18 (x) 2 or 12 (x) 3 or 9 (x) 2 (x) 2 or 3 (x) 3 (x) 4 or 2 (x) 3 (x) 6	M1	Allow on prime factor tree or repeated division
			Condone 18 (×) 2 (×) 1 etc. for this mark
	2 (×) 2 (×) 3 (×) 3	A1	Allow on prime factor tree or repeated division
	$2^2 \times 3^2$	A1ft	ft any product of prime numbers in index form if M1 awarded
5(b)	9	B2	B1 answer 3 or $3^2$ or $3 \times 3$ or $81 = 3^4$ or $3 (\times) 3 (\times) 3 (\times) 3$



Q	Answer	Mark	Comments
6	Line (0900,0) to (1100,80)	B1	need not be straight, but gradient must be positive for all points on the line
	Horizontal line $4\frac{1}{2}$ squares long for stage 2	B1ft	ft from the end of the preceding part of the journey and each stage must be in correct order
	and Horizontal line 1 square across for stage 4		The sections for stages 3 and 5 need not be straight, but gradient must be negative for all points on the line
	Line $\frac{1}{2}$ square across and 3 squares down for stage 3	B1ft	
	line $1\frac{1}{2}$ squares across and down to time axis to represent arriving home for stage 5	B1ft	

7(a)	-10	B2	B1 20 <i>x</i> – 10
			or multiplies out and simplifies with one error
7(b)	<i>a</i> ( <i>a</i> + <i>b</i> + 1)	B2	B1 $a^{2} + a (b + 1)$ or $a (a + b) + a$
			or $a(a+b)+a$
			or $a(a+b+1)$ three terms in bracket with two correct
7(c)	2x > 9 + 1 or $2x > 10$	M1	ое
	x > 5	A1	SC1 ( $x =$ ) 5 or $x <$ 5 or $x \ge$ 5
			or $2x > 8$ and $x > 4$ together

Q	Answer	Mark	Comments
8	12 × 10 or 120(£ or %) or 24 × 6 or 144(£ or %) or 36 × 4 or 144(£ or %)	M1	oe Correct method to calculate comparable values
	120(£ or %) and 144(£ or %) and 144(£ or %)	A1	
	A	Q1ft	Any indication Strand (iii) correct decision based upon their values after M1 awarded

9(a)	4 <i>n</i> + 2	B1	
9(b)	(4n , their $4n+2$ )	B1ft	ft their (a)
9(c)	y = x + 2	B2	oe all equations
	or 4n circled in (a) and $y = x$		B1 $y = mx + c$ with $m = 1$ or $c = 2$
	$-\pi \operatorname{circled} \operatorname{in}(a) \operatorname{and} y = x$		
	$6n$ circled in (a) and $y = \frac{3x}{2}$		
	or		
	$6n + 2$ circled in (a) and $y = \frac{3x}{2} + 2$		

10	445 and 544	B3	B2 445 or 544
			or 450 and 540
			or 450 and 549
			B1 450 or 540 or 545 or 549

11(a)	$x^2 - 5x - 6x + 30$	M1	four terms, three correct with a term in $x^2$ or $x^2 - 11x + k$ with $k \neq 0$
	$x^2 - 11x + 30$	A1	
11(b)	$8a^7b^9$	B2	B1 two correct from 8, $a^7$ and $b^9$ B1 correct answer with multiplication sign(s)



Q	Answer	Mark	Comments
12	$4540000000$ or $4540 \times 10^{6}$	M1	
	4.54(0) × 10 <sup>9</sup>	A1	SC1 their 4 540 000 000, with digits 454, correctly converted to standard form SC1 $4.54(0) \times 10^3$ (million)
			SC1 $4.5 \times 10^9$

13(a)	x <sup>2</sup>	M1	ое
	$\frac{x^2}{x+2x+x^2}$		Condone numerator as $x$ or $2x$
	$\frac{x^2}{3x + x^2} = \frac{x}{x + 3}$ or $\frac{x^2}{x(3 + x)} = \frac{x}{x + 3}$	A1	SC1 chooses a value for <i>x</i> , evaluates the correct numbers of each colour bead and shows that the fraction of blue beads can be written in the form $\frac{x}{x+3}$ eg. <i>x</i> = 3, red = 3, white = 6, blue = 9 and $\frac{9}{18} = \frac{3}{6}$
13(b)	$\frac{x}{x+3} = 0.9$	M1	ое
	x = 0.9x + 2.7 or $0.1x = 2.7$	M1	
	( <i>x</i> =) 27	A1	
	Alternative method 1		
	Chooses a value for <i>x</i> , evaluates the correct numbers of each colour bead and the correct proportion of blue beads.	M1	eg 3, 6, 9 and $\frac{1}{2}$ (oe fraction, decimal or percentage)
	Chooses a value for <i>x</i> , evaluates the correct numbers of each colour bead and the correct proportion of blue beads, for a proportion closer to 90%	M1	eg 3, 6, 9 and $\frac{1}{2}$ (oe fraction, decimal or percentage) and 4, 8, 16 and $\frac{4}{7}$ (oe fraction, decimal or percentage)
	( <i>x</i> =) 27	A1	

Q	Answer	Mark	Comments
	Alternative method 2		
	$\frac{90}{100} = \frac{18}{20}$ or $\frac{36}{40}$ or $\frac{45}{50}$ or $\frac{54}{60}$	M1	
	or $\frac{63}{70}$ or $\frac{72}{80}$ or $\frac{81}{90}$		
	27 30	M1	
	( <i>x</i> =) 27	A1	
14	(2x - y)(2x + y)	B2	B1 $(2x - y)(2x - y)$ or $(2x + y)(2x + y)$ or $(2x - y)^2$ or $(2x + y)^2$ or $(4x + y)(x - y)$ or $(4x - y)(x + y)$
15	Correct equation of any line or associated inequality	M1	Ignore incorrect inequality signs
	Correct equations of all four lines or associated inequalities	M1	Ignore incorrect inequality signs
	$x \ge 3$ and $y > 2$ and $x > y$ and $x + y \le 8$	A1	
	Use of included inequality for at least one of the solid lines	Q1ft	Strand (i) correct use of notation
	and Use of strict inequality for at least one of the dashed lines		



Q	Answer	Mark	Comments
16	$9^{\frac{1}{2}} = 3$ or $(-7)^{\circ} = 1$	B1	
	$\left(\frac{1}{8}\right)^{-\frac{1}{3}} = 8^{\frac{1}{3}}$ or $\frac{1}{\sqrt[3]{\frac{1}{8}}}$ or $\frac{1}{\frac{1}{2}}$ or $\sqrt[3]{8}$	M1	oe $-\frac{1}{2}$ implies M1
	or $\left(\frac{1}{2}\right)^{-1}$ or $\left(\frac{1}{8}\right)^{\frac{1}{3}} = \frac{1}{2}$ or $\sqrt[3]{8} = \frac{1}{2}$		
	$\left(\frac{1}{8}\right)^{-\frac{1}{3}} = 2$	A1	
	All three numbers correctly evaluated and in correct order (-7)°	A1	
	$\left(\frac{1}{8}\right)^{-\frac{1}{3}}$		
	9 <sup>1</sup> / <sub>2</sub>		

Q	Answer	Mark	Comments
17	3(x+2) or $4(x-1)$	M1	Ignore RHS and denominator
	3x + 6 - 4x + 4	M1	Allow one error
			Ignore RHS and denominator
			this also implies first M1 mark
	(x-1)(x+2)	M1	As denominator
	or $x^2 + 2x - x - 2$ or $x^2 + x - 2$		
	$2x^2 + 4x - 2x - 4$ or $2x^2 + 2x - 4$	M1	Ignore LHS
	or $2(x-1)(x+2)$		this also implies third M1 mark
	or $2(x^2 + 2x - x - 2)$ or $2(x^2 + x - 2)$		
	$2x^2 + 3x - 14 = 0$	A1	
	(2x+7)(x-2) (= 0)	M1	Correct method to solve their quadratic equation by
			Correct substitution into the quadratic formula
			or
			Correct completion of the square
			or
			Correct factorisation
	$-\frac{7}{2}$ and 2	A1ft	ft their quadratic but must be exact values (integers, fractions, decimals or surds)
			SC2 $x = -\frac{7}{2}$ or $x = 2$



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