

General Certificate of Secondary Education June 2013

Mathematics

43602H

Unit 2 Higher tier

Final

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from: aqa.org.uk

Copyright © 2013 AQA and its licensors. All rights reserved.

Copyright

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could

lead to a correct answer.

A Accuracy marks are awarded when following on from a correct

method. It is not necessary to always see the method. This can

be implied.

B Marks awarded independent of method.

Q Marks awarded for Quality of Written Communication

ft Follow through marks. Marks awarded for correct working

following a mistake in an earlier step.

Special case. Marks awarded within the scheme for a common

misinterpretation which has some mathematical worth.

M dep A method mark dependent on a previous method mark being

awarded.

B dep A mark that can only be awarded if a previous independent mark

has been awarded.

oe Or equivalent. Accept answers that are equivalent.

eg, accept 0.5 as well as $\frac{1}{2}$

[a, b] Accept values between a and b inclusive.

3.14... Allow answers which begin 3.14 eg 3.14, 3.142, 3.149.

Use of brackets It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

Work not replaced

Erased or crossed out work that is still legible should be marked.

Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

Unit 2 Higher Tier

Q	Answer	Mark	Comments
		I	
1	Sight of 20, 0.5,10 or 2	M1	
	$\frac{20\times0.5}{2}$	M1	oe $\frac{10}{2}$ or 10×0.5 or 20×0.25
	5	A1	
2a	x + 5 or $5 + x$	B1	
2b	x (+) x + 5 (+) x + 10 (+) x + 15 (=54)	B1	oe eg 4x + 30
	their $4x$ + their $30 = 54$	M1	collecting their four or more different algebraic expressions and equating
	their $4x = $ their 24	M1	54 – their 30 correctly evaluated from $ax + b = 54$ with $a > 1$
	6	A1	SC2 6 on answer line with no correct algebraic working
3a	30 p circled	B1	any indication
3b	$4 \times 30 \ (=120)$ or $5 \times 50 \ (=250)$ or $4 \times 0.3(0)(=1.20)$ or $5 \times 0.5(0)(=2.50)$	M1	Oe
	their 120 + their 250 or 370 or their 1.2(0) + their 2.5(0) or 3.7(0)	M1	
	(£)3.70	Q1	Strand (i) Do not accept 3.7 or (£)3.70p SC2 (£)3.50 must be supported by 1.50 + 2.00 SC1 350 must be supported by 150 + 200

Q	Answer	Mark	Comments
4	$(\frac{1}{4} \text{ and})\frac{2}{4}$ or $\frac{2}{8} \text{ and } \frac{4}{8}$ or 25(%) and 50(%) or 0.25 and 0.5	M1	oe into equivalent form fractions with common denominator or percentages or decimals
	$\frac{1.5}{4}$	A1	oe eg $\frac{37.5}{100}$ or 37.5% or 0.375
	$\frac{3}{8}$	Q1	oe fraction Strand (ii)
	Alternative method		
	$\frac{1}{4} + \frac{1}{2} \ (= \frac{3}{4})$	M1	
	$\frac{3}{4} \times \frac{1}{2}$	A1	ое
	$\frac{3}{8}$	Q1	oe fraction Strand (ii)
5a	6x + 12 or 2x + 2	M1	
	6 <i>x</i> + 12 + 2 <i>x</i> + 2	A1	
	8 <i>x</i> + 14	A1ft	oe ft from their 4 terms
5b	x(x-11) or $(x-11)x$	B1	
6	Meets all 4 criteria $(x =) 64 \text{ and } (y =) 27$ or $(x =) 81 \text{ and } (y =) 64$	B3	B2 Their 2 values meet any 3 criteria B1 Their 2 values meet any 2 criteria B1 Reversed $(x =) 27$ and $(y =) 64$ B1 Reversed $(x =) 64$ and $(y =) 81$ SC2 $(x =) 8^2$ and $(y =) 3^3$ with no working SC2 $(x =) 9^2$ and $(y =) 4^3$ with no working SC1 a two digit square number subtract either 27 or 64 SC1 full list of two digit squares 16,25,36,49,64,81 with 27 and 64

Q	Answer	Mark	Comments
7a	$4x \le 13 + 7 \text{ or } x - \frac{7}{4} \le \frac{13}{4}$	M1	oe
	<i>x</i> ≤ 5	A1	SC1 $x < 5$ or $x = 5$ or $x \ge 5$
7b	3 8	B2	B1 for
			or
8	2a + 4b or $3a + 6b$	M1	
	2a + 4b and $3a + 6b$	M1	
	2(a+2b) or $3(a+2b)$	A1	
	or $\frac{2}{3}$ with no evidence of incorrect working		
	$\frac{2(a+2b)}{3(a+2b)}$ (=) $\frac{2}{3}$	Q1	Strand (ii) must see factorisation
9	$\frac{35}{100} \times 600 \ (= 210)$	M1	oe 100 – 35 (= 65)
	600 – their 210 (= 390)	M1	oe $600 \times \text{their } \frac{65}{100} (= 390)$
	their 390 ÷ 5 (= 78)	M1	oe
	312	A1	
	Alternative method		
	100 – 35 (= 65)	M1	oe
	their 65 ÷ 5 (=13)	M1	oe
	their 65 – their 13 (=52)	M1	oe $\frac{their\ 13}{100} \times 600\ (=78)$
	or 100 – (35 + their 13) (=52)		or $\frac{their\ 48}{100} \times 600\ (=288)$
	312	A1	

Q	Answer	Mark	Comments
10a	y = -1.5x + 3	В3	oe $3x + 2y = 6$
			5 . 2 ,
			B2 $y = 1.5x + 3$
			B2 $-1.5x + 3$
			B2 $y = -1.5x + c$
			B1 $y = mx + 3$
			B1 $y = 1.5x + c$
			B1 $1.5x + 3$
			B1 $-\frac{3}{2}$ oe
10b	y = 3x - 9	B2	oe
			B1 $y = 3x + c$; c not 4
			B1 $3x - 9$
			B1 $-3 = 3 \times 2 + c$
11	$180 \times 5 \ (= 900) \text{ or } 180 \times \frac{10}{9} = (200)$	M1	oe
	180 × 3 (= 900) 01 180 × 9 = (200)		
	their 900 is $\frac{9}{10}$ or		oe $\frac{9000}{9}$ or 100×10
		M1dep	9
	their $900 \times \frac{10}{9}$ or their 200×5		
	1000	A1	
	Alternative method		
	$\frac{1}{5} \times \frac{9}{10} \ (= \frac{9}{50}) \ \text{or} \ 5 \times \frac{10}{9} \ (= \frac{50}{9})$	M1	
	their $\frac{9}{50}$ is 180 or	M1 dep	
	$180 \times \text{their } \frac{50}{9}$		
	1000	A1	
12	2 [M1	2 - T 2 - T 2
	$w-3=\sqrt{t}$	1411	or $\sqrt{t} = w - 3$ or $(w - 3)^2$ or $-\sqrt{t} = 3 - w$
	$t = (w-3)^2$	A1	oe ignore fw
			SC1 $t = (w + 3)^2$

Q	Answer		Mark	Comments
13	2x + 3y = 53 $9x - 3y = 57$	6x + 9y = 159 6x - 2y = 38	M1	oe Allow one error
	11 <i>x</i> = 110	11 <i>y</i> = 121	M1	
	x = 10 or y = 11		A1	
	x = 10 and y = 11		A1	
	Alternative metho	od		
	y = 3x - 19	$x = \frac{y+19}{3}$	M1	oe Allow one error
	2 <i>x</i> +3(3 <i>x</i> -19)=53	$\frac{2(y+19)}{3} + 3y = 53$	M1	
	11x - 57 = 53	11y + 38 = 159		
	x = 10 or y = 11		A1	
	x = 10 and $y = 11$		A1	
14a	1		B1	
14b	$\frac{1}{5^3}$ or $\frac{1}{125}$ or 0.	2 × 0.2 × 0.2	M1	$\left(\frac{1}{5}\right)^3$ or 125^{-1} or 0.2^3
	0.008 or $\frac{8}{1000}$		A1	
	8 × 10 ⁻³		A1 ft	ft Any decimal 0 < x < 1 correctly converted to standard form
15	$8x^2 - 12xy - 10xy$	+ 15y ²	M1	Allow one term error
	$8x^2 - 12xy - 10xy$	+ 15y ²	A1	
	$8x^2 - 22xy + 15y^2$		A1 ft	ft their four terms if M1 awarded Do not ignore fw for final mark

Q	Answer	Mark	Comments
16a	$\sqrt{4}$	M1	$\frac{2\sqrt{2}}{\sqrt{2}}$ or $\frac{\sqrt{8}}{\sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}}$ or $\sqrt{\frac{8}{2}}$ or $\sqrt{\frac{4}{1}}$ or $\frac{\sqrt{16}}{2}$
			or $\frac{\sqrt{8}\sqrt{2}}{2}$ or $\frac{2}{1}$
	2	A1	
16b	two correct steps	M1	eg two of:
			$\sqrt{4} = 2$ or $\sqrt{1} = 1$ or cancels $\sqrt{5}$ or combines any two surds
	$\sqrt{144}$	M1	oe eg $\sqrt{12}\sqrt{12}$ or $\sqrt{4}\sqrt{36}$
	k = 12	A1	
17a	x + 7.5 or $7.5 + x$	B1	$x + 7\frac{1}{2}$
17b	x(x + 7.5) = 2(x + x + 7.5)	M1	ft their x + 7.5 from (a) in the form x + c for all 4 method marks
	$x^2 + 7.5x = 4x + 15$	M1	
	$x^2 + 3.5x - 15 = 0$	M1	
	or $2x^2 + 7x - 30 = 0$		
	(2x-5)(x+6) (=0)	M1	
	2.5 and 10	A1	either order but in correct pairs
	and		
	-6 and 1.5		SC1 one correct pair