

5. Above the Earth's surface, the magnitude of the gravitational force on a particle due to the Earth is inversely proportional to the square of the distance of the particle from the centre of the Earth. The Earth is modelled as a sphere of radius R and the acceleration due to gravity at the Earth's surface is g . A particle P of mass m is at a height x above the surface of the Earth.

(a) Show that the magnitude of the gravitational force acting on P is

$$\frac{mgR^2}{(R+x)^2} \quad (3)$$

A rocket is fired vertically upwards from the surface of the Earth. When the rocket is at height $2R$ above the surface of the Earth its speed is $\sqrt{\left(\frac{gR}{2}\right)}$. You may assume that air resistance can be ignored and that the engine of the rocket is switched off before the rocket reaches height R .

Modelling the rocket as a particle,

(b) find the speed of the rocket when it was at height R above the surface of the Earth. (9)

7.

Diagram **NOT**
accurately drawn

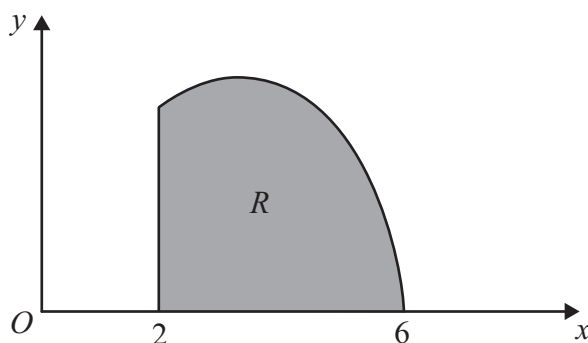


Figure 1

The shaded region R is bounded by the curve with equation $y = \frac{1}{2}x(6-x)$, the x -axis and the line $x=2$, as shown in Figure 1. The unit of length on both axes is 1 cm. A uniform solid P is formed by rotating R through 360° about the x -axis.

(a) Show that the centre of mass of P is, to 3 significant figures, 1.42 cm from its plane face. (9)

The uniform solid P is placed with its plane face on an inclined plane which makes an angle θ with the horizontal. Given that the plane is sufficiently rough to prevent P from sliding and that P is on the point of toppling when $\theta = \alpha$,

(b) find the angle α . (4)

Given instead that P is on the point of sliding down the plane when $\theta = \beta$ and that the coefficient of friction between P and the plane is 0.3,

(c) find the angle β . (3)



