

General Certificate of Education (A-level) June 2012

Mathematics

MD01

(Specification 6360)

Decision 1

Mark Scheme

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Key to mark scheme abbreviations

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
В	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation
√or ft or F	follow through from previous incorrect result
CAO	correct answer only
CSO	correct solution only
AWFW	anything which falls within
AWRT	anything which rounds to
ACF	any correct form
AG	answer given
SC	special case
OE	or equivalent
A2,1	2 or 1 (or 0) accuracy marks
−x EE	deduct x marks for each error
NMS	no method shown
PI	possibly implied
SCA	substantially correct approach
c	candidate
sf	significant figure(s)
dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

Q				Soluti	ion			Marks	Total	Comments
1 (a)		1	2	3	4	5	6			
	\boldsymbol{A}	0	0	1	0	0	0	M1		6×6 matrix labelled with some 0, 1,
	B	1	0	0	1	0	0			✓, × 's (at least 9 entries)
	C	0	0	1	0	0	1			
	D	1	1	0	0	0	0	A1	2	All correct
	E F	0 0	0	0	1 0	1 1	0			
	Г	U	U	U	U	1	1			
(b)	A-3	3+C						M1		
	or									
	2-I	D+1								
	A-3	S+C-	6+F	-5 + 1	E - 4 +	B-1	+D-2	A1		
	or		D 4				2 4			
	2-L)+1-	B + 4 -	-E+5	-F+	6 – C	+3-A			
	Match A3, B1, C6, D2, E4, F5							B1	3	
	1.1000		, 21, 0	, 0, 2	-,,					
							Total		5	
2(a)	1st	1						B2		All correct
	2nd	2 }						22		The contect
	3rd	1						(B1)	2	2 correct
		-)								
(b)	1st	1)								
(6)								B2		All correct
	2nd	2						(D1)	2	2
	3rd	0]						(B1)	2	2 correct
(c)	No, l	nas to	check	23 (aı	nd 26)			E1	1	No, (at least) one more pass needed etc
							Total		5	
1							Total		3	

Q	Solution	Marks	Total	Comments
3(a)(i)	$ \begin{array}{c c} AD & 4 \\ AB & 6 \\ AC & 16 \end{array} $	M1		Using Prims, first 3 edges correct, 6+ edges, no cycles, must have edges not lengths
	DE 19 EG 10	B1		8 edges
	GI 12	A1		GI 6 th
	IH 13 17 17	A1	4	All correct
(ii)	97	B1	1	
(iii)	$\nearrow B$ F	M1		ST with 6+ edges
	$A \stackrel{D}{\longleftarrow} E \stackrel{G}{\longleftarrow} I$	A1	2	All correct including labels
	C H			
(b)(i)	IF	B1	1	
(ii)	AC	B1	1	
	Total		9	
4(a)(i)	B 6 3433 G	M1		Dijkstra, $2+$ values at C and 1 value at B and D
	10 1817 16 24 29 44 43 0 10 9 8 39 C E F H	A1		Sight of 10, 9, 8 (only) at <i>C</i>
		m1		3 values at E and 2 values at G or I
	$V_{\overline{7}}$ 36 $\overline{35}$ V I	A1		All correct, including crossing out, boxing (condone omission of 0 at <i>A</i>)
		B1	5	39 at <i>J</i> (final value)
(ii)	Route A D C E F H I J	B1	1	or reverse
(b)	(Time = 39 min) their 39			
	(Dist =) $\frac{their39}{60} \times 90$ OE	M1	_	
	= 58.5 km CAO	A1	2	Must see km, or 58500 m SC 58.5 with no working scores M1A0, but 58.5 km with no working scores 2/2
	Total		8	

Q	Solution	Marks	Total	Comments
5(a)	BD+FH = 210+210 = 420 BF+DH = 200+180 = 380	M1		These 3 sets of pairs
	$BH+DF = \begin{bmatrix} 260+180 \\ 260+340 \end{bmatrix} = 600$	A2,1		3 correct totals, 2 correct totals
	(MIN) = 2430 + 380	m1		2430 + their smallest of three pair totals
	= 2810	A1	5	CSO
(b)	2430 + 340 (DF) = 2770	B1F	1	2430 + their <i>DF</i>
(c)(i)	2430 + 180 (DH) = 2610	B1F	1	2430 + their min (must have scored M1)
(ii)	B, F only	B1	1	
	Total		8	
6(a)		E1	1	
(b)(i)	28	B1		
(ii)	Odd number of edges at (all) vertices	E1	2	Must see the word odd, not just 7
(c)(i)	$\frac{n(n-1)}{2}$ OE	В1		
(ii)	n-1	B1		
(iii)	n must be odd	E1		Must have <i>n</i> in their answer
(iv)	n = 3	B1	4	Must have n in their answer
	Total		7	

Q	Solution	Marks	Total	Comments
7(a)	$ \begin{pmatrix} A & C & F & D & E & B & A \\ 10 & 31 & 32 & 11 & 18 & 16 \end{pmatrix} $			
	= 118	B1	1	
(b)	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	M1 m1 A1 B1	4	Tour from A visiting at least 4 vertices Visits all vertices Correct order from A
(c)	$ \begin{array}{c cccc} (18) & E & (11) & D & (14) \\ B & & & & & & & & & & & & \\ & & & & & & &$	M1		Spanning tree + 2 different edges from <i>A</i> (ST must be edges using <i>B</i> , <i>C</i> , <i>D</i> , <i>E</i> , <i>F</i> not lengths, but condone two lengths from <i>A</i> , or 26) Diagram is not necessary in part (c)
	$_{F}ackslash$	A1		Correct minimum spanning tree
	$ \begin{array}{c} B \\ \hline \begin{bmatrix} 16 \end{bmatrix} \\ A \end{array} $	A1		Correct edges (not lengths) from A
	= 100	B1	4	
(d)	B C A	B1		Correctly labelled diagram
	Lower bound does not make a cycle OE AND tour > 100	E1	2	Both, must be strict inequality
	Total		11	

Q		Solutio	n		Marks	Total	Comments
8(a)	A B 1 1	C 1 1	D 1 2				
	3	6	2.52.67	AWRT	M1 A1		At least 3 evaluated values for D 3 rd value of D as 2.5
	4	24	2.71	AWRT	B1 m1 A1		Values of (1), 1, 2, 6, 24 (only) seen for <i>C</i> Exactly 5 evaluated values for <i>D</i> Correct 5 values for <i>D</i>
	An estimate o	of e is 2.71	AWRT	•	A1 CSO	6	All correct values seen (1 for <i>A</i> , 4 for <i>B</i> , 5 for <i>C</i> and <i>D</i>) and correct final statement
(b)	Never-ending $(A,)$ $B(,C)$ ϵ		et to 1 C	ЭE	B2,1	2	
				Total		8	

Q	Solution	Marks	Total	Comments
9(a)	$x \ge 100, \ y \ge 200$ $x + y + z \ge 400$ OE	В1		
	$4x + 3y + 4z \le 1800$ OE	B1		
	$y \ge \frac{40}{100} \left(x + y + z \right) \text{OE}$	B1	3	
(b)(i)	(x=2z)			
	$x + y + \frac{1}{2}x \ge 400$ $\Rightarrow 3x + 2y \ge 800$	M1		Correct substitution and fully simplifying 1 inequality (must see evidence: either replacing z or multiplying inequality)
	$ 4x + 3y + 2x \le 1800 6x + 3y \le 1800 2x + y \le 600 $	A1		As above 'in 2 nd inequality'
	$5y \ge 2x + 2y + x$ $3y \ge 3x$ $y \ge x$	A1	3	As above 'in 3 rd inequality'
(ii)				Each line must be straight to have the B mark available. For all lines, must be correct to half square horizontal and vertical at the indicated vertices.
	500	B1		x = 100, y = 200
	400 Max (100,400)	B1		y = x line
	300 FR	B1		through (100, 100) and (200, 200) $2x + y = 600$ line
	200	B1		through (100, 400) and (200, 200) $3x + 2y = 800$ line
	100 200 300	В1	5	through (100, 250) and (200, 100) Feasible Region, all lines correct and region labelled (condone no shading, ignore 'poor' shading)
(iii)	(Max) $y + \frac{3}{2}x$	M1		PI by objective line with gradient –1.5
	(=400+150)=550	A1	2	
(iv)	Buys 100 soft 400 medium 50 firm	В1	1	
	Total		14	
	TOTAL		75	