

**General Certificate of Education (A-level) January 2011** 

**Mathematics** 

**MD01** 

(Specification 6360)

**Decision 1** 

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from: aqa.org.uk

Copyright © 2011 AQA and its licensors. All rights reserved.

## Copyright

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

## **Key to mark scheme abbreviations**

m or dM mark is dependent on one or more M marks and is for method A mark is dependent on M or m marks and is for accuracy B mark is independent of M or m marks and is for method and accuracy E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)  dp decimal place(s)	M	mark is for method
B mark is independent of M or m marks and is for method and accuracy E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	m or dM	mark is dependent on one or more M marks and is for method
E mark is for explanation  √or ft or F follow through from previous incorrect result  CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	A	mark is dependent on M or m marks and is for accuracy
CAO correct answer only CSO correct solution only AWFW anything which falls within AWRT anything which rounds to ACF any correct form AG answer given SC special case OE or equivalent A2,1 2 or 1 (or 0) accuracy marks -x EE deduct x marks for each error NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	В	mark is independent of M or m marks and is for method and accuracy
CAO correct answer only  CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	E	mark is for explanation
CSO correct solution only  AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	√or ft or F	follow through from previous incorrect result
AWFW anything which falls within  AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	CAO	correct answer only
AWRT anything which rounds to  ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	CSO	correct solution only
ACF any correct form  AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	AWFW	
AG answer given  SC special case  OE or equivalent  A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	AWRT	anything which rounds to
SC special case OE or equivalent A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	ACF	any correct form
OE or equivalent A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	AG	answer given
A2,1 2 or 1 (or 0) accuracy marks  -x EE deduct x marks for each error  NMS no method shown  PI possibly implied  SCA substantially correct approach  c candidate  sf significant figure(s)	SC	special case
-x EEdeduct x marks for each errorNMSno method shownPIpossibly impliedSCAsubstantially correct approachccandidatesfsignificant figure(s)	OE	or equivalent
NMS no method shown PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	A2,1	2 or 1 (or 0) accuracy marks
PI possibly implied SCA substantially correct approach c candidate sf significant figure(s)	–x EE	deduct x marks for each error
SCA substantially correct approach c candidate sf significant figure(s)	NMS	no method shown
c candidate sf significant figure(s)	PI	possibly implied
sf significant figure(s)	SCA	substantially correct approach
8 8 0	c	candidate
dp decimal place(s)	sf	significant figure(s)
	dp	decimal place(s)

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

## **MD01**

MIDUI				
Q	Solution	Marks	Total	Comments
1(a)				
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1		$(6\times6)$ matrix labelled with
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			some $\sqrt{s}$ or $\times s$ or 0's or 1's or $-s$
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			Some v s or x s or o's or r s or - s
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$			
	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	A1	2	CAO
		711	2	CHO
(b)	A-4+E			
	A-5+B	M1		1 correct
	C-4+E $6-D+2$			
	6-D+2	M1		1 correct, from a different start point
	6-B+5			
	1-F+3			
	4-5+R-3+F-1			
	A-5+B-3+F-1 C-4+E-2+D-6	A1		Either order
	C - 4 + E - 2 + D - 6	A1		Either order
	or			
	first			
	A-4+E-2+D-6	(A1)		
	then }			Must be in this order
	C-4+A-5+B-3+F-1	(A1)		
	or			
	first			
	A-5+B-6	(A1)		
	then	(211)		Must be in this order
		(4.1)		iviust de ili ulis diuei
	C-4+E-2+D-6+B-3+F-1	(A1)		
	M . 1 . 45 . P2 . C4 . P. C . P2 . P3	D.1	_	
	Match A5, B3, C4, D6, E2, F1	B1	5	Must be stated (not solely on diagram)
	Total		7	

MD01 (cont	D01 (cont)						
Q	Solution	Marks	Total	Comments			
2(a)	7	B1		A correct pivot (7 or 22)			
	22	B1	2	2 <sup>nd</sup> correct pivot and no others			
(b)	C						
	1st 7	B1					
	2nd 5	B1	_	Condone 7, 5, 3 or $7 + 5 + 3 = 15$			
	3rd   3	B1	3	unlabelled but must be in this order			
(-)	N- 16 10 h?t h	Г.1	1	DOTH (91-2) (			
(c)	No – 16, 19 haven't been compared (OE)	E1	1	BOTH "No" (or equiv) AND "16, 19"			
	Total		6	(only) mentioned or highlighted in script			
3(a)(i)		M1	0	Prim's, MST, 6+ edges (no cycles), edges			
3(a)(i)	$EB  \left(\begin{array}{c} 5 \end{array}\right)$	IVI I		not lengths or vertices, with first 2 edges			
	<i>EH</i>   7			correct			
	$AB \mid 8 \mid$			Concec			
	HI   9	В1		8 edges			
				1 1 1 2 1 1			
	$AD \mid 10$	<b>A</b> 1		AB 3rd			
	$DG \mid 4 \mid$						
	<i>EF</i>   12	<b>A</b> 1	4	All correct			
	$FC = \begin{pmatrix} 6 \end{pmatrix}$						
(ii)	61	В1	1				
		21	-				
(iii)	A B C						
		M1		6+ edges, connected, no cycles			
	D $E$ $F$						
			_				
	$\bigcup_{G}$ $\bigcup_{H}$ $I$	A1	2	Correct, including labelling			
	g n						
(b)	Dalata RA RE and reconnect with 1 adas	<b>N</b> /I 1		PI from their diagram in (iii)			
(0)	Delete <i>BA</i> , <i>BE</i> and reconnect with 1 edge or	M1		r i nom men magram m (m)			
	a spanning tree with 7 edges not including						
	B (either as a list or diagram)						
	2 (State) as a list of diagram)						
	(61 - 13 + 11) = 59	<b>A</b> 1	2	Note: 59 scores 2/2			
	Total		9				

MD01 (cont				
Q	Solution	Marks	Total	Comments
4(a)(i)	2.5 Ju.5	M1		(2 values at E or F)
	9 4.5 3	A1		Correct values at E and F
	A 7.5 C 6 H 6 J 13.5 3 Y	m1		2 values at <i>I</i>
	0 13.5 2t 19.5 188	m1		3 values at $J$
	10.5 F13-512 3	B1		18 at <i>J</i>
	7.5 7.8	A1	6	All correct, condone 0 missing at A, with rejected values crossed and final values boxed and no extra values at other vertices
(ii)	ADFIJ	B1	1	or reverse
(b)	7.5+ $x$ <12 OE 16.5+ $x$ $\geqslant$ 18 OE	M1		Either correct condone $7 \cdot 5 + x \le 12$ or $16 \cdot 5 + x > 18$
	10.5+x ≥18 OE	A1		Both correct
	$1.5 \leqslant x < 4.5$	A1	3	$1.5 \leqslant x < 4.5$ seen (with or without working) scores $3/3$ Condone $1.5 \leqslant x$ and $x < 4.5$ or exact equiv in words but must see "and"
				$1.5 < x \text{ or } 1.5 \leqslant x \text{ or } x < 4.5 \text{ or } x \leqslant 4.5$
				with no working M1A0
	Total		10	
5(a)	A vertex / vertices of odd order (A, B, G, H) OE	E1	1	Condone statement of non-Eulerian graph
(b)	AB + GH = (180 + 165) = 345 AG + BH = (90 + 210) = 300	M1		These 3 correct sets of pairs
	AH + BG = (150 + 210) = 360	A2,1		3 correct totals, 2 correct totals
	Dist 1215 + 300 PI = 1515	M1 A1	5	1215 + their smallest CSO
(c)(i)	3	B1	1	
(ii)	2	B1	1	
(11)	Total		8	

MD01 (cont				
Q	Solution	Marks	Total	Comments
6(a)(i)	10	B1	1	
400		D.1		
(ii)	4	B1	1	
	_	D.1		
(iii)	5	B1	1	
<i>a</i> .)				
(b)	eg			
		M1		Simple graph, 6 vertices
		1V1 1		Simple graph, 6 vertices
		A1	2	Eulerian graph with 9 edges
		711	2	Buterian graph with 5 eages
	Total		5	
7(a)	33	B1	1	
			-	
(b)	BAEDCB	M1		Tour that visits all vertices
		<b>A</b> 1		Correct tour
	= 41	B1	3	
(c)	$A \qquad (3) \qquad B$			Spanning tree without <i>C</i>
	/			(either drawn or edges listed)
	(4)			
	(10)	M1		and
	E D			2 different edges from <i>C</i>
				(either drawn or edges listed)
	A.			
		<b>A</b> 1		C AMOT
		AI		Correct MST
	D			
	(11)			
		A1		Correct 2 edges from C
	(5)	111		Correct 2 edges from C
	č			
	= 33	B1	4	
(d)	$A \longrightarrow B$			
	D			
	E	M1		Correct network
				Possibly earned in (c)
	č			
	Optimal OE	A1	2	
	Total		10	

MD01 (cont	()					
Q			Marks	Total	Comments	
8(a)						
	X	A	B			
	0					Condone omission of $X = 0$ , $A = 20$ , $B = 8$
		20	8			
		10				
			16	M1		SCA Trace as far as their '10' at A and
		5				their '16' at B, ignore values in X column
			32	A1		All correct up to and including 32 at B
	32					
		2				
			64	A1		All correct up to and including 64 at <i>B</i>
		1				
			128			
	160			A1	4	All correct and no further working
	("160")					
	361010		0.5	D.1		
(b)	Multiplication	l	OE	B1	1	
			OF	F1		
(c)	Continuous lo		OE	E1	2	
	as never reach	Line 90	OE	E1	2	
			Total		7	

MD01 (cont)		126.	700 · 3	
Q	Solution	Marks	Total	Comments
9(a)	$6x + 9y + 9z \le 600$ $2x + 3y + 3z \le 200$	M1		Any of the three inequalities correct (un)simplified, condone strict inequalities
	$2x + 3y + 3z \le 200$ $9x + 6y + 9z \le 600$	A1		CAO
	$3x + 2y + 3z \le 200$	A1		CAO
	•	AI		CAO
	$6x + 12y + 18z \ge 480$			
	$x + 2y + 3z \ge 80$	A1	4	CAO
(b)(i)	(z=y)	2.54		
	$2x+3y+3y \le 200$ or $2x+6y \le 200$	M1		Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$x + 3y \le 100 $ AG			
	$3x + 2y + 3z \le 200$			Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$(\Rightarrow) 3x + 5y \le 200 \qquad AG$			
	$x + 2y + 3z \ge 80$			Correctly substitute into <b>this</b> inequality - either simplified or unsimplified form
	$(\Rightarrow) x + 5y \ge 80$ AG	A1	2	All correct – must link their original inequality to the stated answers
(ii)	Each line must be straight to have the B ma For all lines, must be correct to ½ square ho			al at the indicated vertices.
	50	B1		Line through (10, 30) and (40, 20)
	30	B1		Line through (50, 10) and (0, 40)
	20 FR	B1		Line through (80, 0) and (0, 16)
	10 0 20 40 60 80 100 120 x	B1	4	FR, must have all lines correct and labelled region (condone no shading)
(iii)	Max  x + 2y   PI	M1		If no statement (PI), then check OL on diagram, which must be correct for M1
	Max (= 25 + 50) = 75	A1	2	Note: 75 with no working 2/2
(iv)	25 basic, 25 standard, 25 luxury	B1F	1	Condone "25 of each type" ONLY if (b)(iii) fully correct Note $x = 25 = y = z$ B0
	Total		13	11000 N 25 y 2 D0
	TOTAL		75	
	IUIAL	13		